

A visualization of particle tracks, likely from a detector, showing a dense cluster of yellow and green lines radiating from a central point, with some blue and red spots scattered throughout. The background is dark with a greenish glow.

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# SPECIAL TOPICS IN EXPERIMENTAL PARTICLE PHYSICS

Lecture 4: Beauty is in the details

# LOOKING FOR NEW PHYSICS?

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Want to open a deathly locked safe?



Through  
**high energy**...?



Through  
**high precision**...?

# LOOKING FOR NEW PHYSICS?

## ■ Through **HIGH ENERGY**:

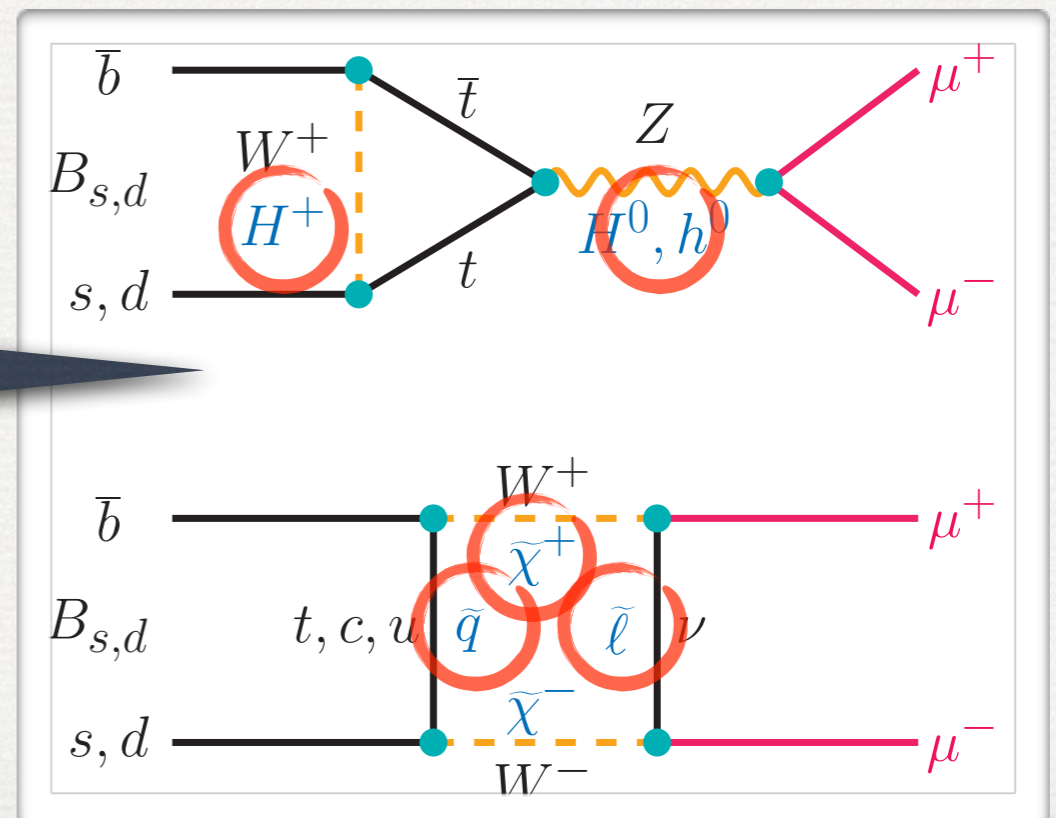
- Produce “**real**” new particles and can be discovered via their decays or any other interactions with the detectors.

## ■ Through **HIGH PRECISION**:

- “**Virtual**” new particles participate in the loop processes and can be discovered by seeing any deviations from the Standard Model.

If these particles cannot be observed in the direct searches, this is the place one shall still look for!

*Both direct and indirect searches are necessary and complement each other!*



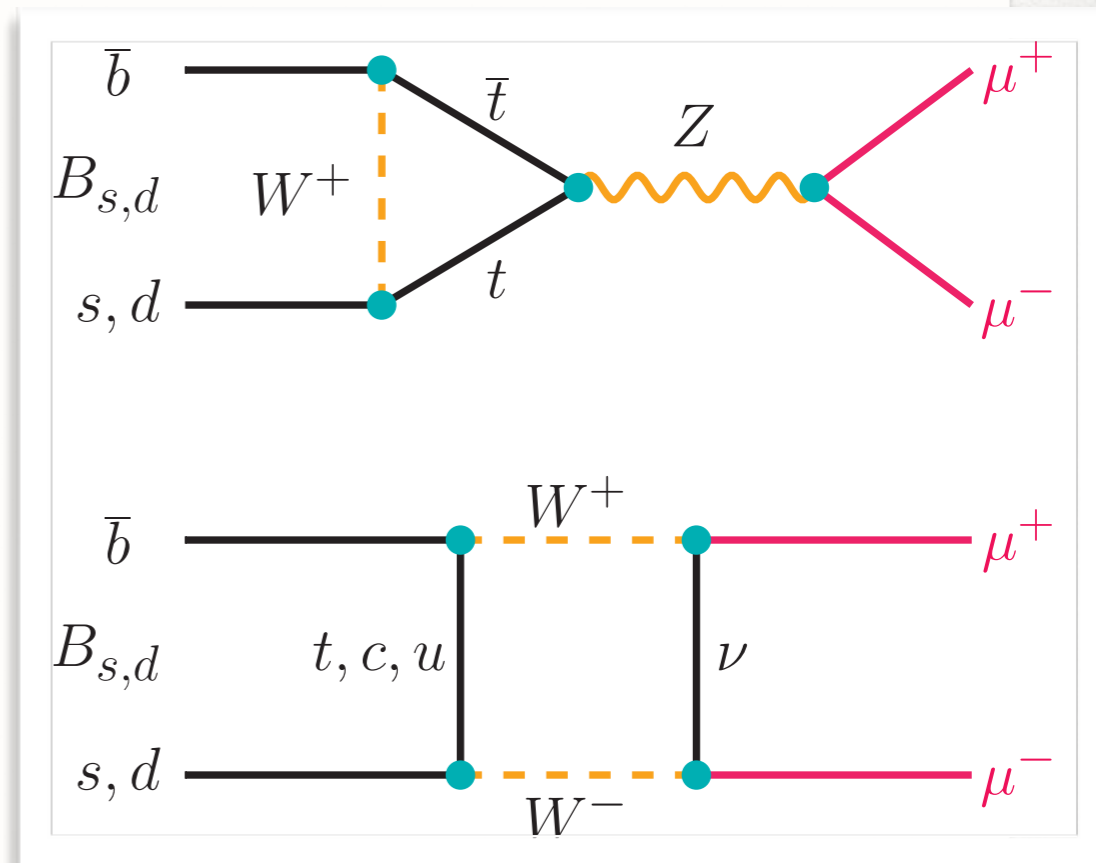
# THE PHYSICS: $B_{s,d} \rightarrow \mu^+ \mu^-$

- In the Standard Model,  $B_{s,d} \rightarrow \mu^+ \mu^-$  decays are highly suppressed:
  - FCNC processes, only proceed through Z-penguin, and box diagrams (suppressed by  $[m_W/m_t]^2$ ).
  - Cabibbo suppressed:  $|V_{tq}|^2$
  - Helicity suppressed:  $[m_\mu/m_B]^2$
- Resulting **tiny branching fractions**, ( $\sim 1/300M$ ) but rather *robust*:

$$B(B_s \rightarrow \mu^+ \mu^-) = (3.65 \pm 0.23) \times 10^{-9}$$

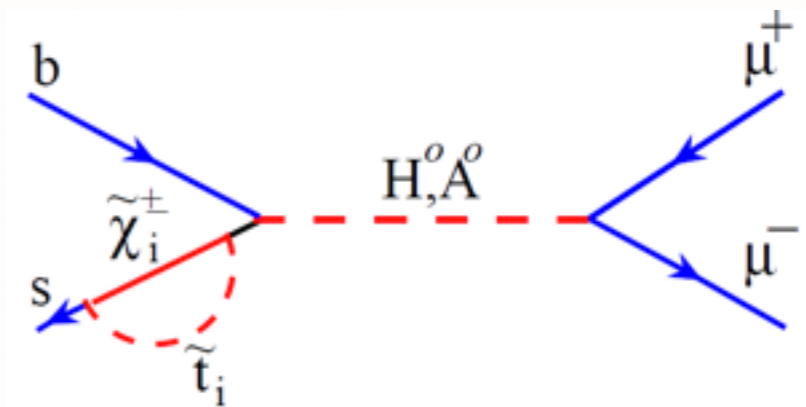
$$B(B_d \rightarrow \mu^+ \mu^-) = (1.06 \pm 0.09) \times 10^{-10}$$

Ref: Bobeth et al, PRL 112, 101801 (2014)



# THE PHYSICS: $B_{s,d} \rightarrow \mu^+ \mu^-$

- Loop diagram + Suppressed SM + Theoretically clean = *An excellent place to look for new physics.*

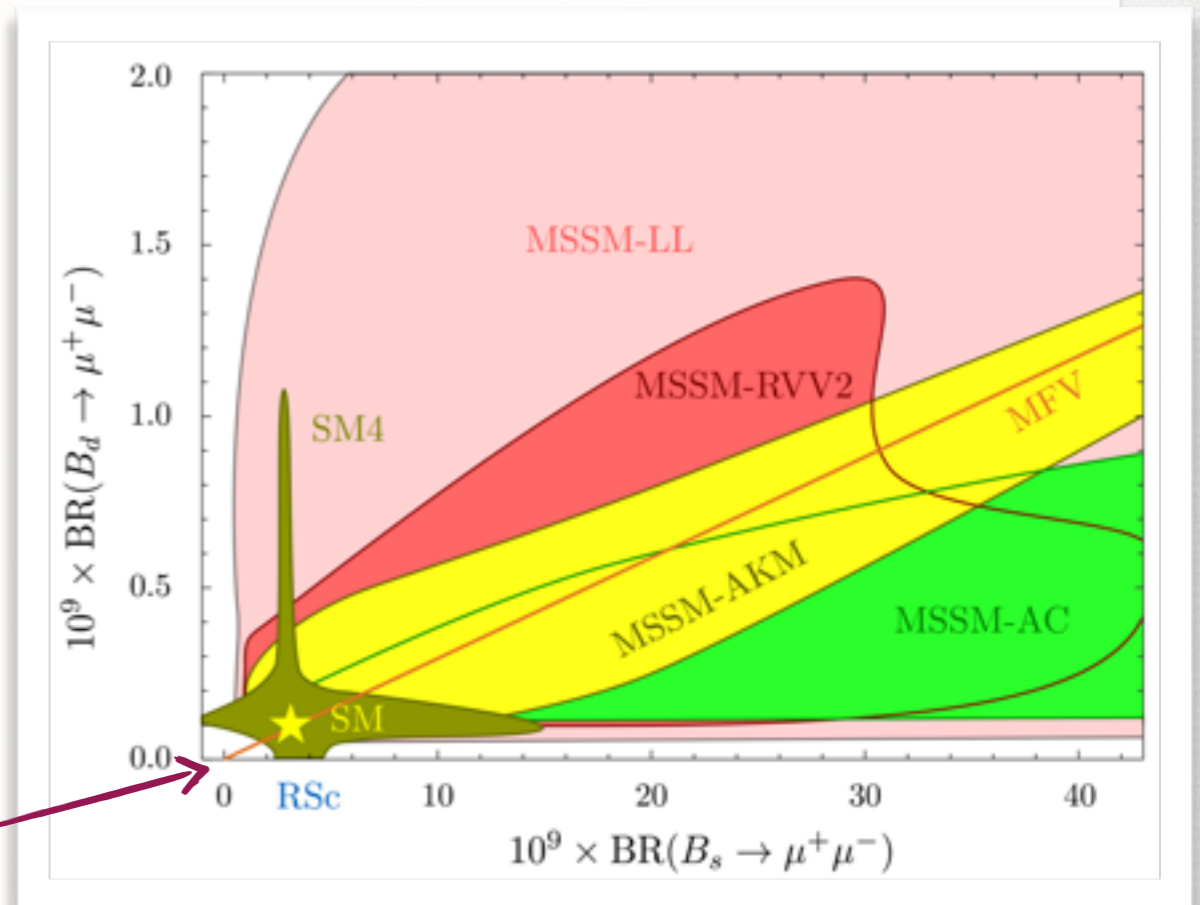


- Sensitive to extended Higgs sectors  $\Rightarrow$  Constrains NP parameter spaces.

- Some of the new physics scenarios may boost the  $B \rightarrow \mu\mu$  decay rates by 10~20 times easily, for example:

- 2HDM:  $B \propto \tan^4\beta$  &  $m(H^+)$
- MSSM:  $B \propto \tan^6\beta$

- $B_s/B_d$  ratio – a stringent test of minimal flavor violation hypothesis.

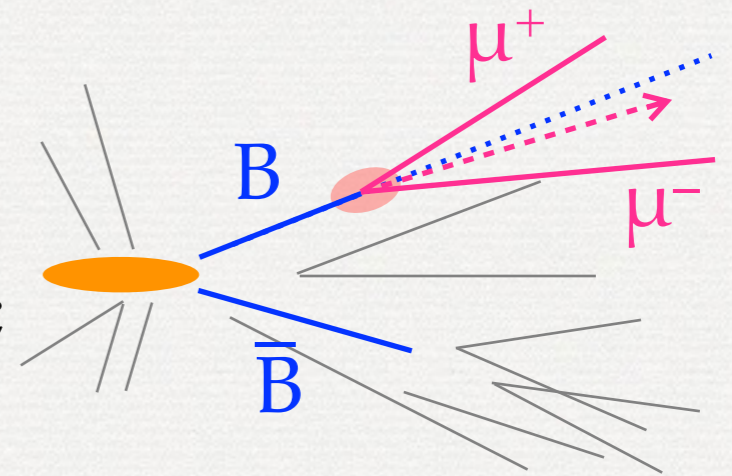


Ref: D. M. Straub, arXiv: 1012.3893

# ANALYSIS ASPECTS

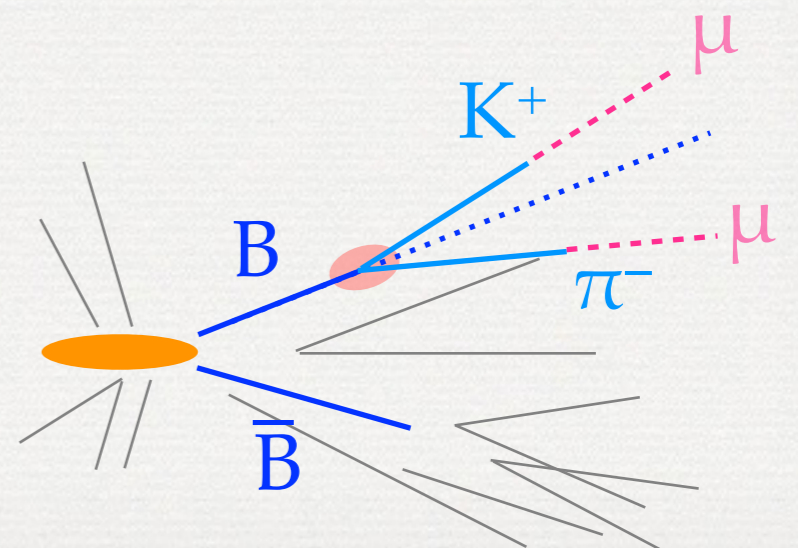
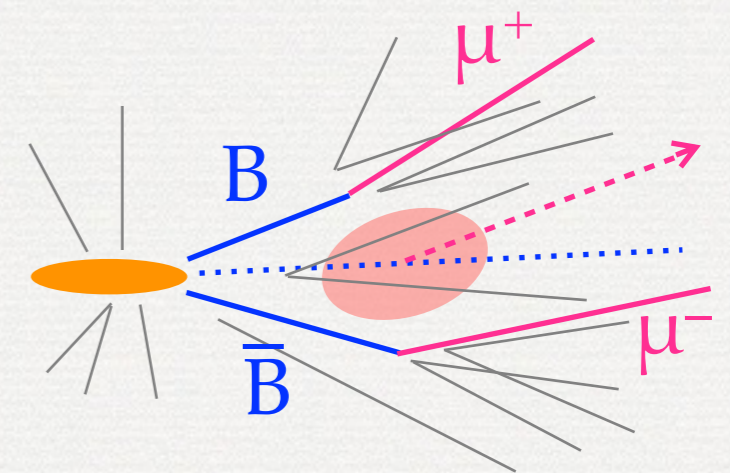
## ■ The $B_{s,d} \rightarrow \mu^+ \mu^-$ signal

- two muons from one displaced vertex; momentum aligned with its flight direction; invariant mass peaking at  $M(B_{s,d})$ .



## ■ Background sources

- two semileptonic B decays
- one semileptonic B + a misidentified hadron
- rare background from single B meson decays: e.g.  $B \rightarrow K\pi/KK$  (peaking),  $B_s \rightarrow K^- \mu^+ \nu$  (not peaking)



Powerful background suppression reached by **muon quality**, **well-reconstructed secondary vertex**, **isolation**, **pointing angle**, and  **$M(\mu\mu)$  resolution**.

# ANALYSIS ASPECTS (II)

- Event classification is carried out by **Boosted Decision Tree (BDT)** method by including several topological and kinematical variables for background suppression.
- Calibrations / validations with  $B^+ \rightarrow J/\psi K^+$ ,  $B^0 \rightarrow K^- \pi^+$  and  $B_s \rightarrow J/\psi \phi$ .
- Normalized to the reference channel  $B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^+$  (LHCb also take  $B^0 \rightarrow K \pi$  as normalization):

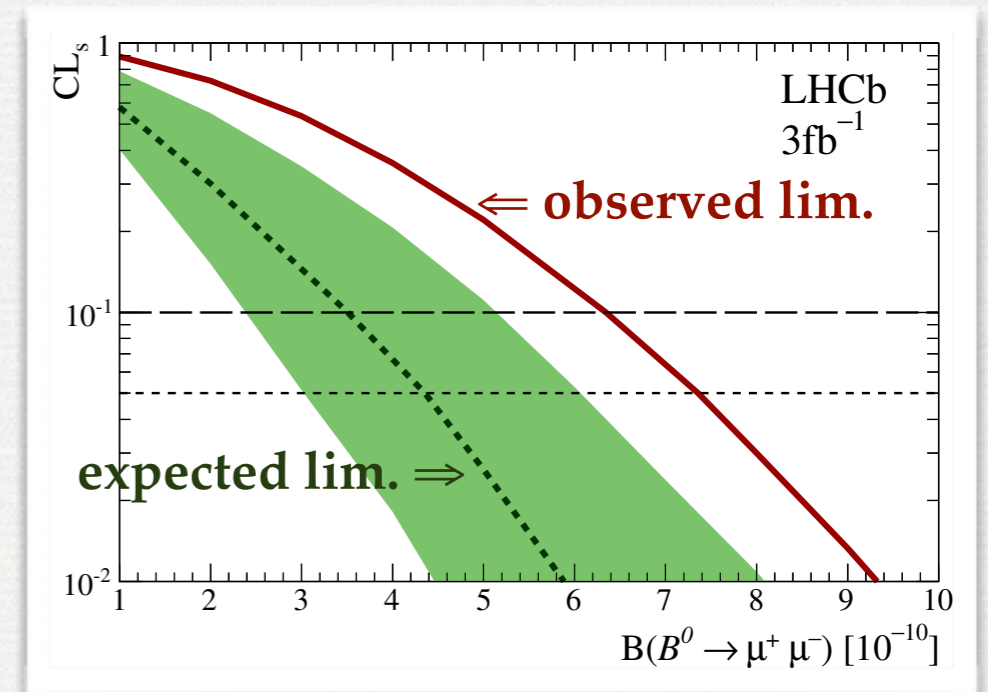
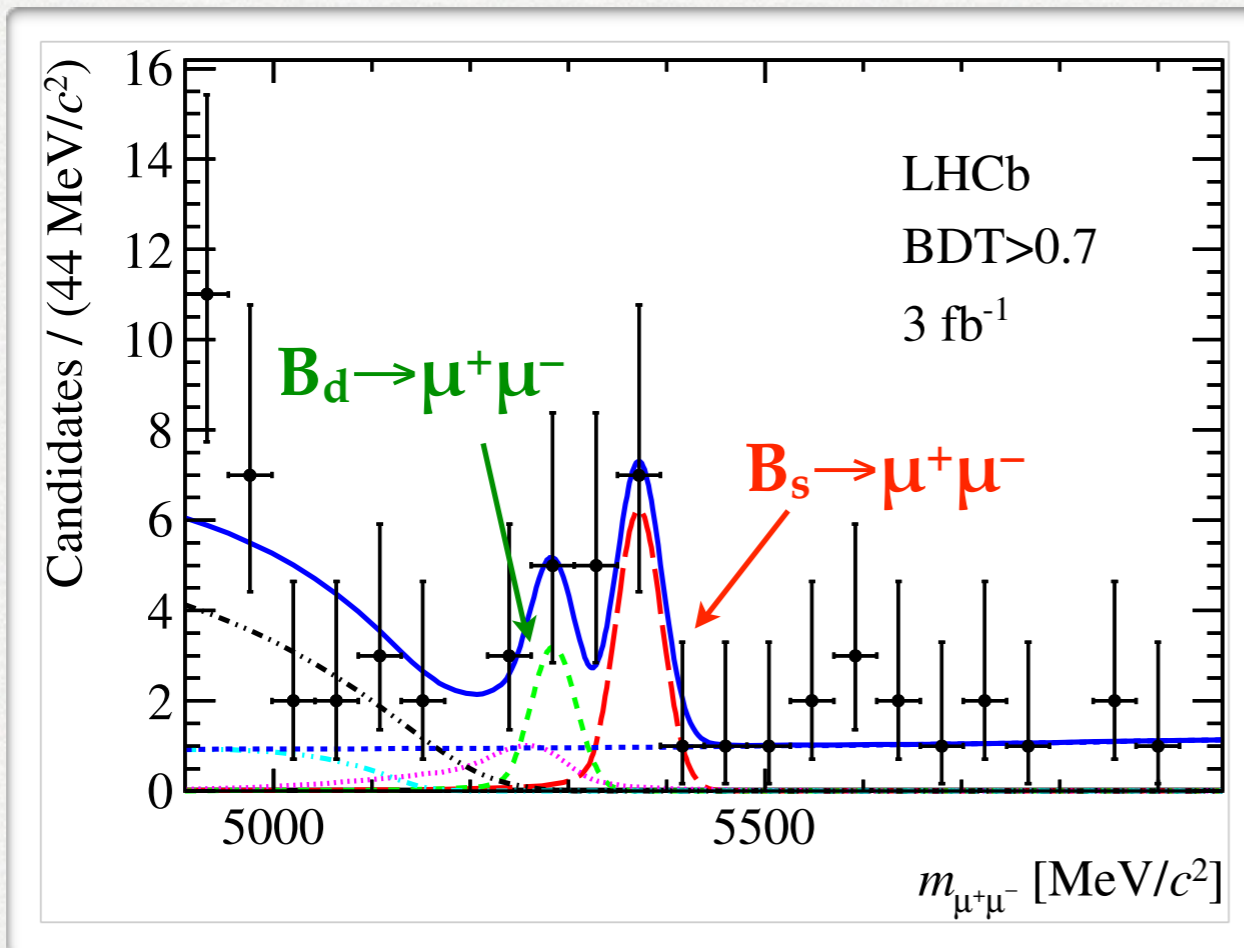
$$\mathbf{B}(B_{s,d} \rightarrow \mu^+ \mu^-) = \frac{N_s}{N(B^\pm \rightarrow J/\psi K^\pm)} \times \mathbf{B}(B^\pm \rightarrow J/\psi K^\pm) \times \frac{A(B^\pm)}{A(B_s)} \frac{\varepsilon^{ana}(B^\pm)}{\varepsilon^{ana}(B_s)} \frac{\varepsilon^\mu(B^\pm)}{\varepsilon^\mu(B_s)} \frac{\varepsilon^{trig}(B^\pm)}{\varepsilon^{trig}(B_s)} \frac{f_u}{f_s}$$

Acceptance  $\longrightarrow$   $A(B^\pm)$   
 Selection efficiency  $\longrightarrow$   $\varepsilon^{ana}(B^\pm)$   
 muon identification  $\longrightarrow$   $\varepsilon^\mu(B^\pm)$   
 Trigger efficiency  $\longrightarrow$   $\varepsilon^{trig}(B^\pm)$   
 B-hadronization composition  $\longrightarrow$   $f_u$   
 (LHCb JHEP 04 (2013) 001: 0.256±0.020)

Similar trigger & selection for reducing systematics

# LHCb RESULTS: $B_{s,d} \rightarrow \mu^+ \mu^-$

- LHCb updated the analysis with full dataset ( $\sim 3 \text{ fb}^{-1}$ ) with an improved BDT; the results are consistent with the predictions.
- The significance for  $B_s \rightarrow \mu\mu$  decay is  $4.0\sigma$  ( $5.0\sigma$  expected).



↑ An upper limit on the decay rate of  $B_d \rightarrow \mu\mu$  is given.

Channel	Branching fraction
$B_s \rightarrow \mu^+ \mu^-$	$(2.9^{+1.1}_{-1.0}) \times 10^{-9}$
$B_d \rightarrow \mu^+ \mu^-$	$< 7.4 \times 10^{-10} @ 95\% \text{ CL}$

ref. LHCb PRL 111 (2013) 101805



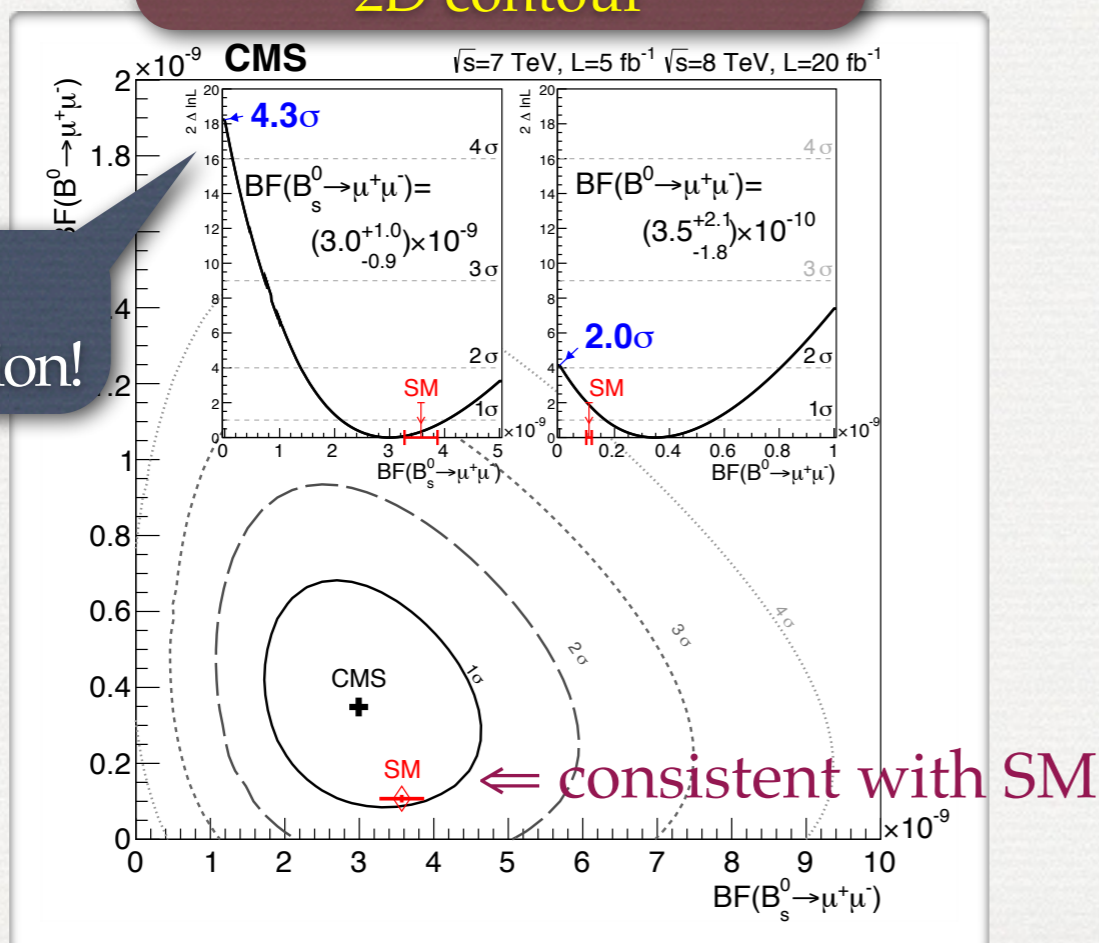
# CMS RESULTS: $B_{s,d} \rightarrow \mu^+ \mu^-$

- Branching fractions extraction with unbinned maximum likelihood fit in 12 categorized BDT bins.
- A simpler “1D-BDT” fit is used as a cross check.

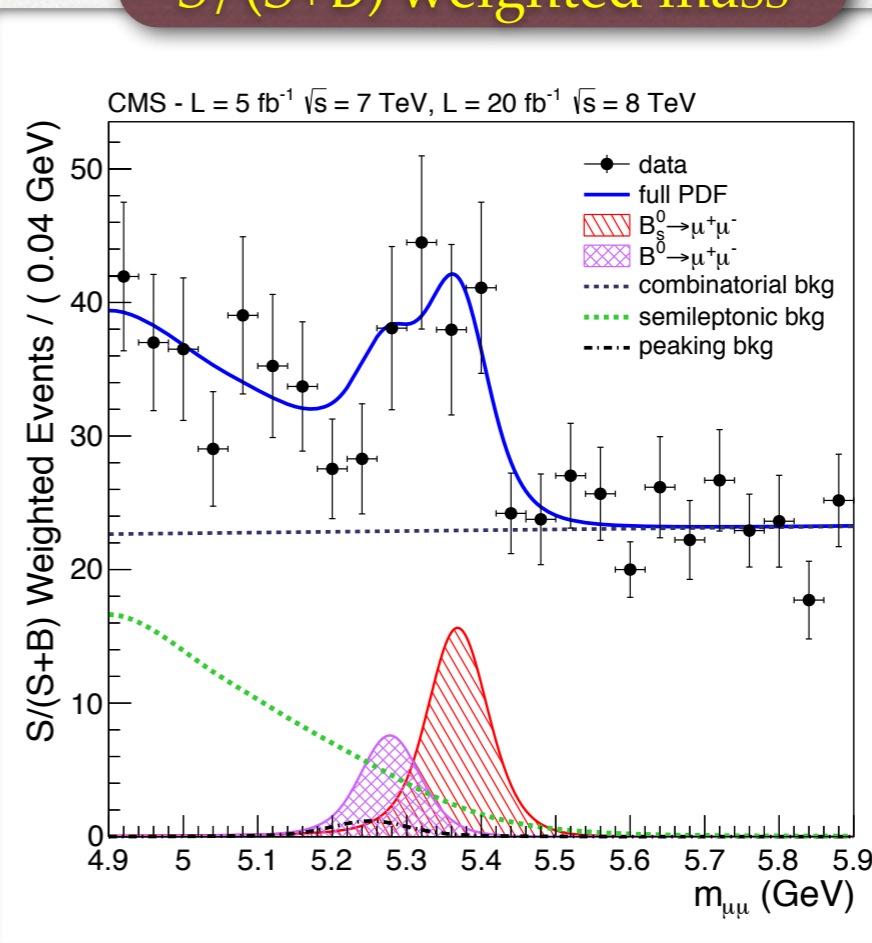
Ref. CMS PRL 111 (2013) 101804

Channel	Branching fraction
$B_s \rightarrow \mu^+ \mu^-$	$(3.0^{+1.0}_{-0.9}) \times 10^{-9}$
$B_d \rightarrow \mu^+ \mu^-$	$< 1.1 \times 10^{-9}$ @ 95% CL

## 2D contour

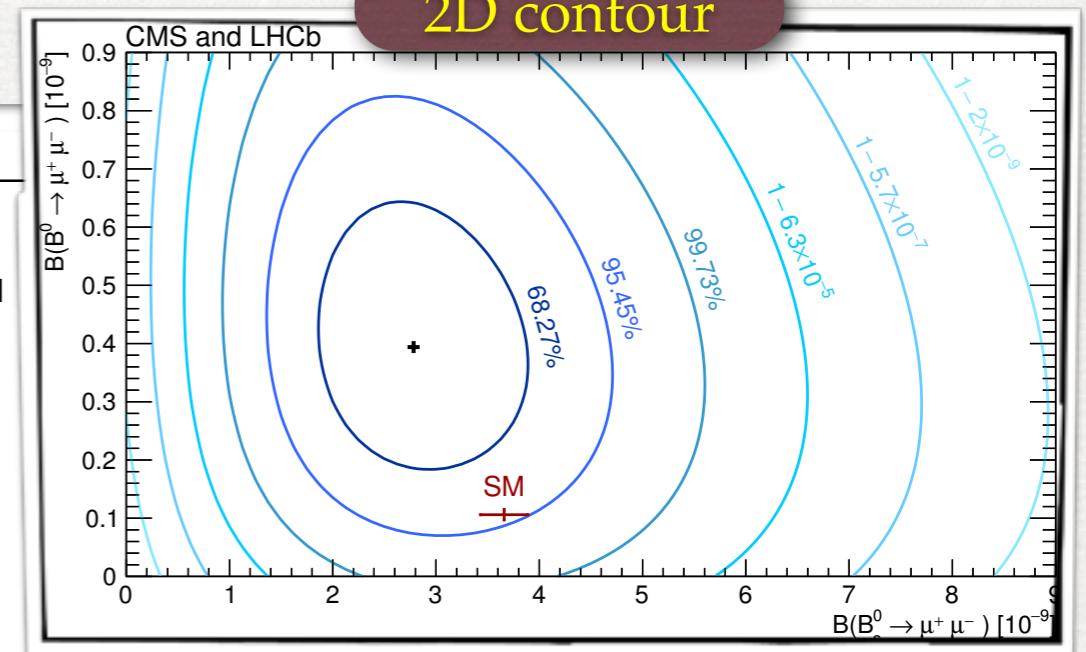
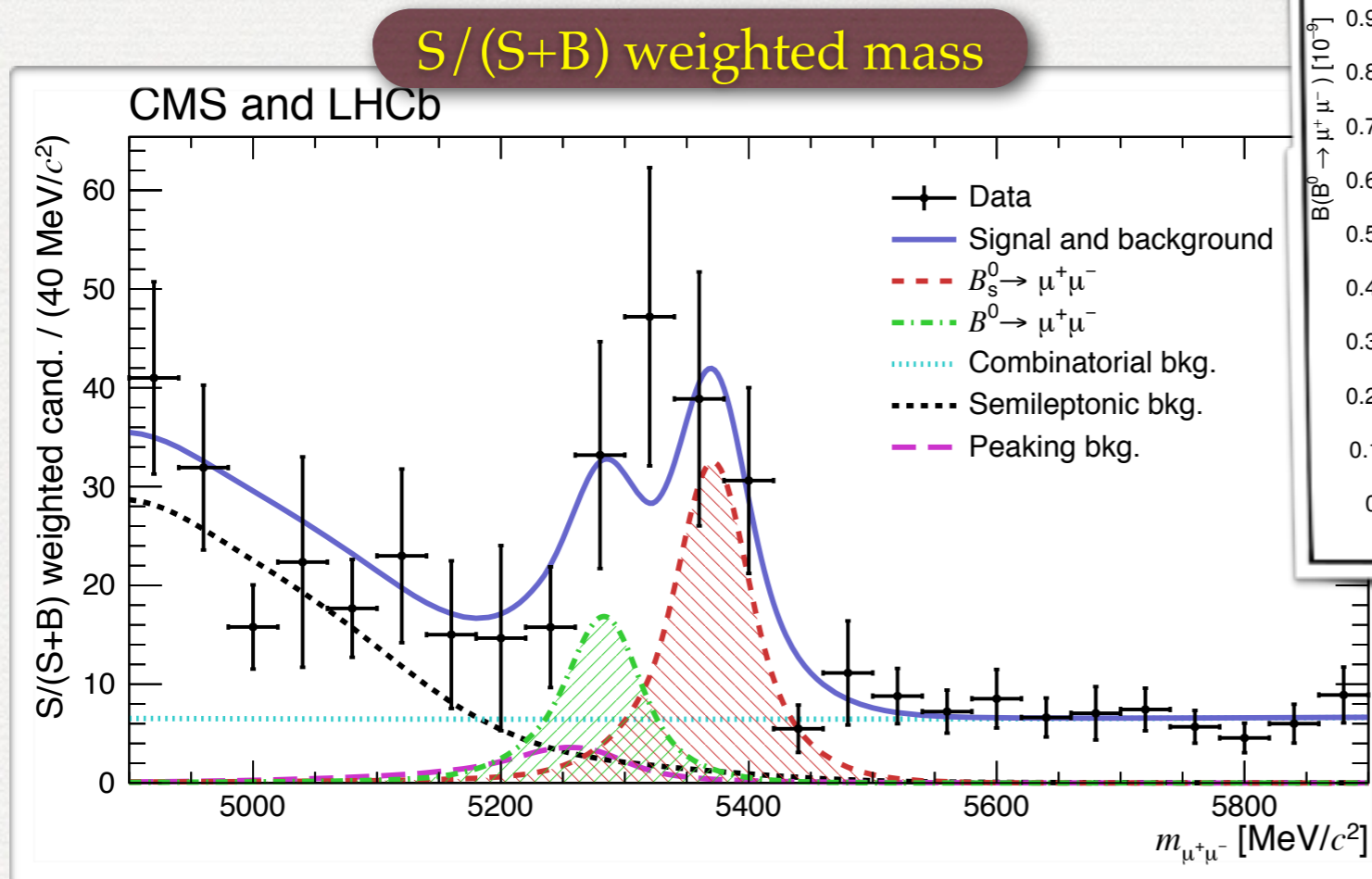


## S/(S+B) weighted mass



# CMS+LHCb COMBINATION

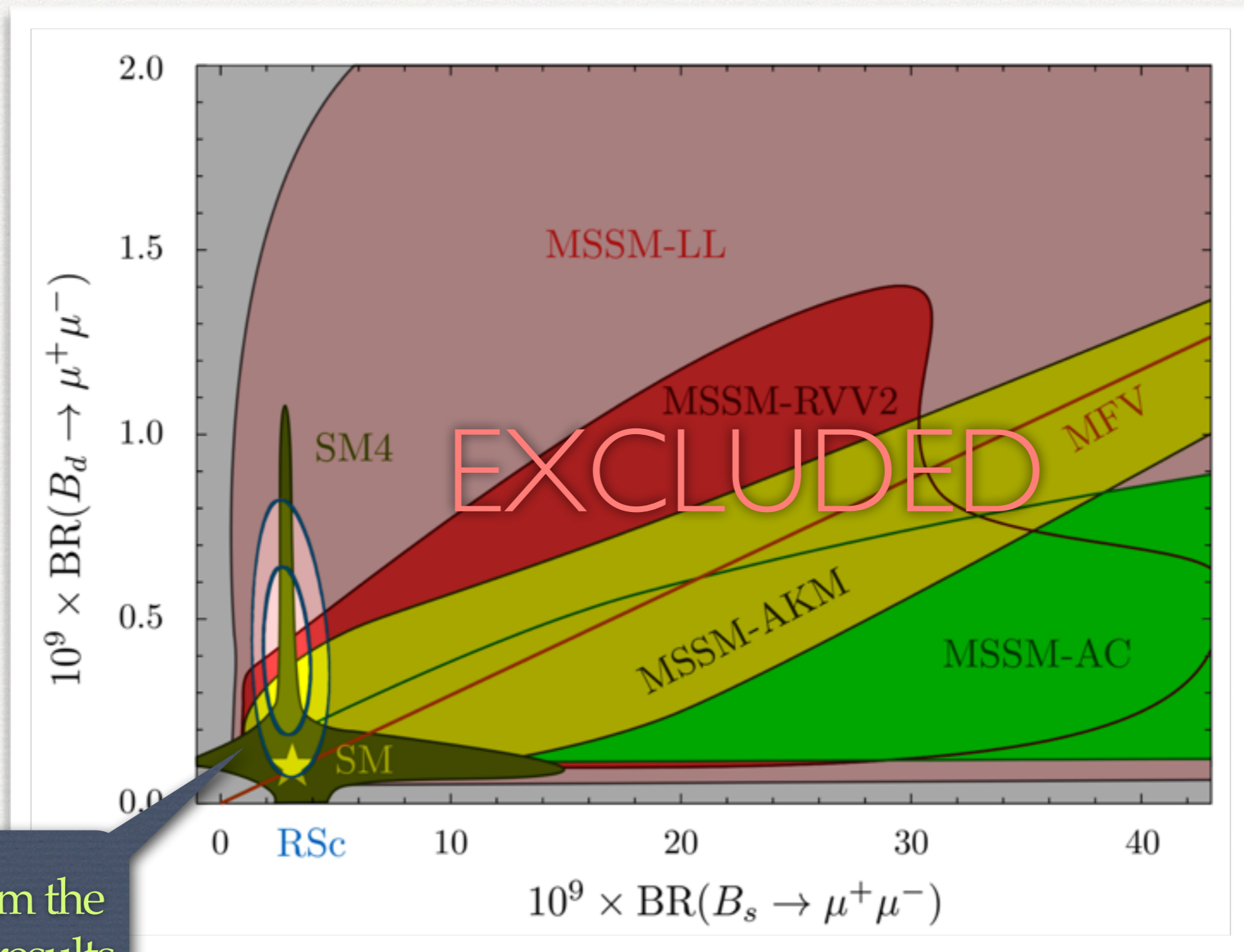
- A full combination for CMS and LHCb analyses for  $B_{s,d} \rightarrow \mu^+\mu^-$  at likelihood level has been carried out.
- The observed significance for  $B_s \rightarrow \mu^+\mu^-$  is  $6.2\sigma$ ; it also produces  $3\sigma$  evidence for an excess of events in the search for  $B_d \rightarrow \mu^+\mu^-$  decays.



Channel	Branching fraction
$B_s \rightarrow \mu^+\mu^-$	$(2.8^{+0.7}_{-0.6}) \times 10^{-9}$
$B_d \rightarrow \mu^+\mu^-$	$(3.9^{+1.6}_{-1.4}) \times 10^{-10}$

The combined paper is in preparation, targeting Nature.

# CMS+LHCb COMBINATION

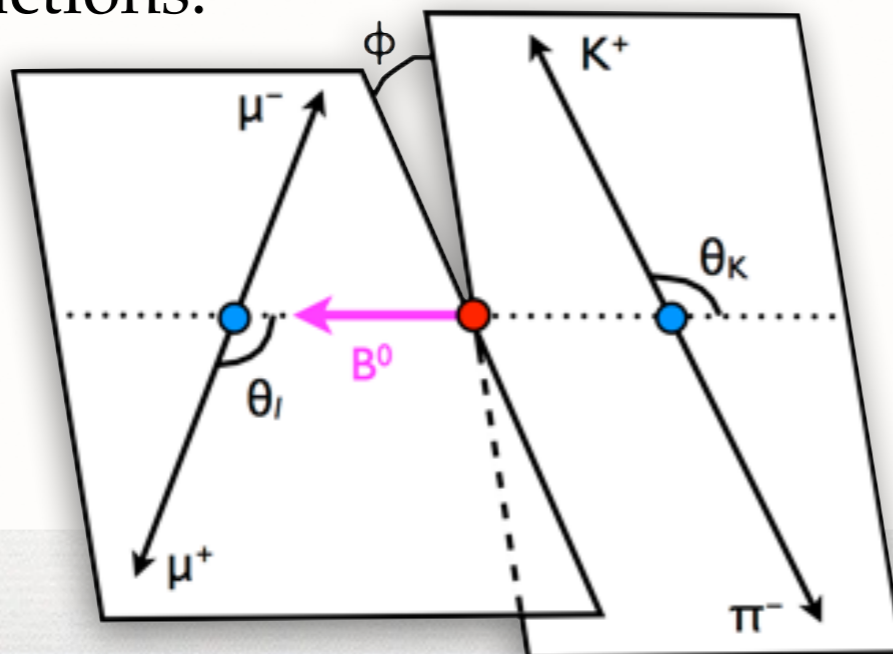
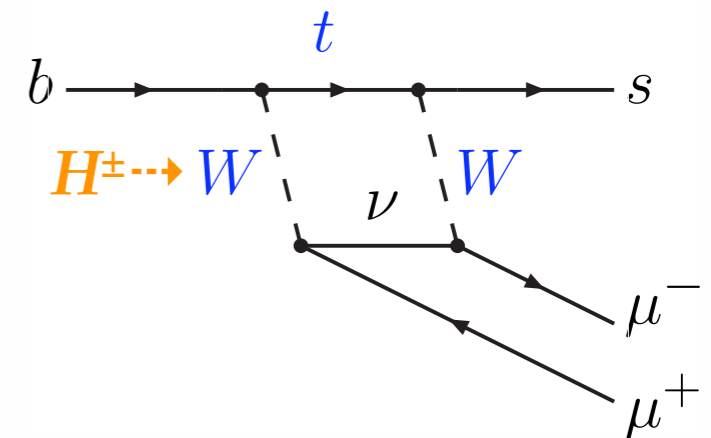
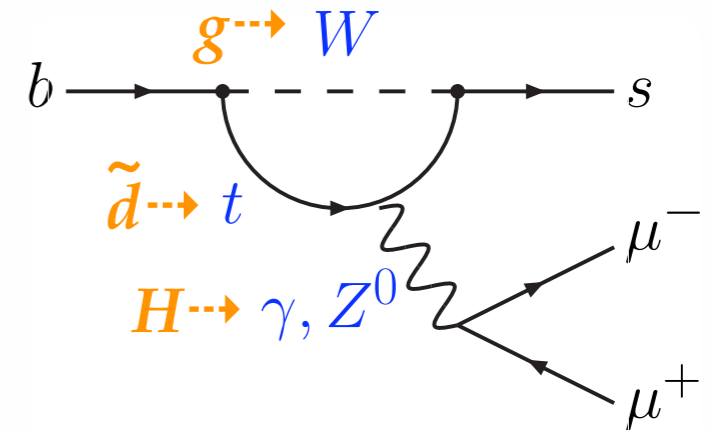


Contours from the combination results

# ANGULAR ANALYSIS OF

$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$

- The  $B \rightarrow K^* \mu \mu$  decay is proceed with **FCNC** process, **sensitive to new physics beyond the Standard Model**.
- Robust theoretical calculations.
- Single channel with many measurements (and as a function of  $q^2$ ): branching fractions,  $A_{FB}$ , polarization,... etc., which allows detailed tests of the structure of the underlying interactions.



Four-particle final states lead to 3 angular observables ( $\theta_K, \theta_L, \phi$ ).

# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ MODEL

- The full angular distribution actually depends on 11 different terms:

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1}{4}(1 - F_L) \sin^2\theta_K \cos 2\theta_\ell + F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + \cancel{S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi} + \cancel{S_5 \sin 2\phi_K \sin \theta_\ell \cos \phi} + S_6 \sin^2\theta_K \cos \theta_\ell + \cancel{S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi} + \cancel{S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi} + S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right]$$

LHCb: drop 4 terms by folding  $\phi \rightarrow \phi + \pi$  for  $\phi < 0$

Parameters ( $S_3, S_6, S_9, \dots$ ) can be converted to ordinary parameters ( $A_{FB}, F_L$ , etc.) + S-wave modeling in addition.

- Alternatively by integrating out 1 or 2 angles to reduce the model:

$$\frac{d^3\Gamma}{d\cos\theta_K d\cos\theta_L dq^2} = \frac{9}{16} \left\{ \left[ \frac{2}{3} F_S + \frac{4}{3} A_S \cos\theta_K \right] (1 - \cos^2\theta_L) + (1 - F_S) \left[ 2F_L \cos^2\theta_K (1 - \cos^2\theta_L) + \frac{1}{2}(1 - F_L)(1 - \cos^2\theta_K)(1 + \cos^2\theta_L) + \frac{4}{3} A_{FB} (1 - \cos^2\theta_K) \cos\theta_L \right] \right\}$$

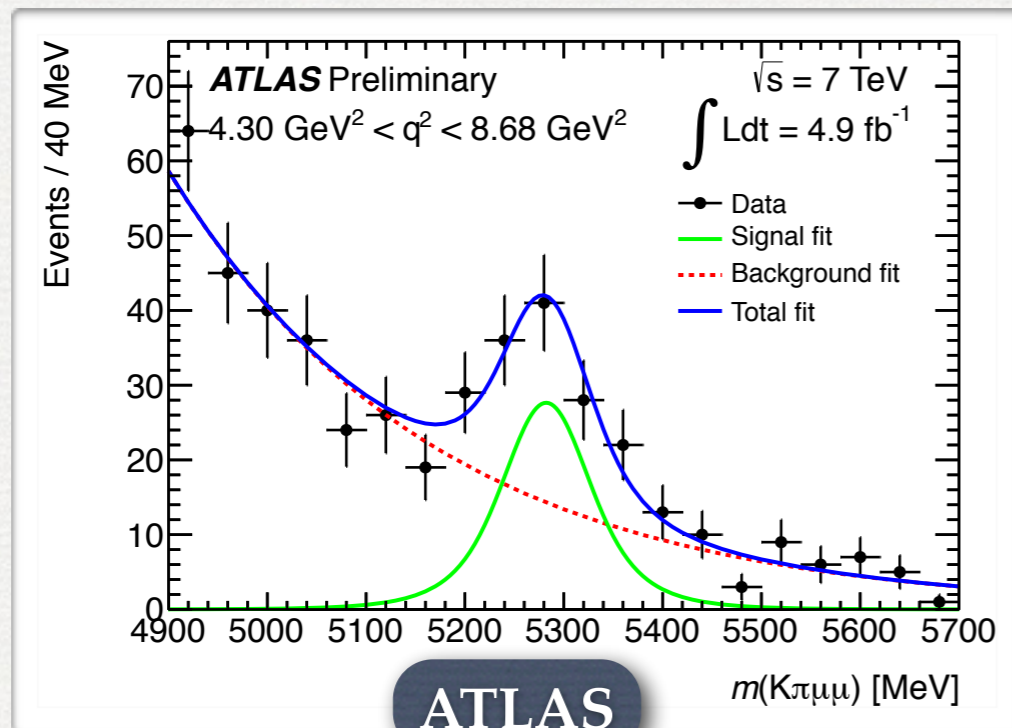
CMS: integrated out  $\phi$   
(and adding S-wave)  
ATLAS: further integrated out  $\theta_K$  or  $\theta_L$



Extract physics parameters ( $F_L, A_{FB}$ , etc.) in bins of  $q^2$ .

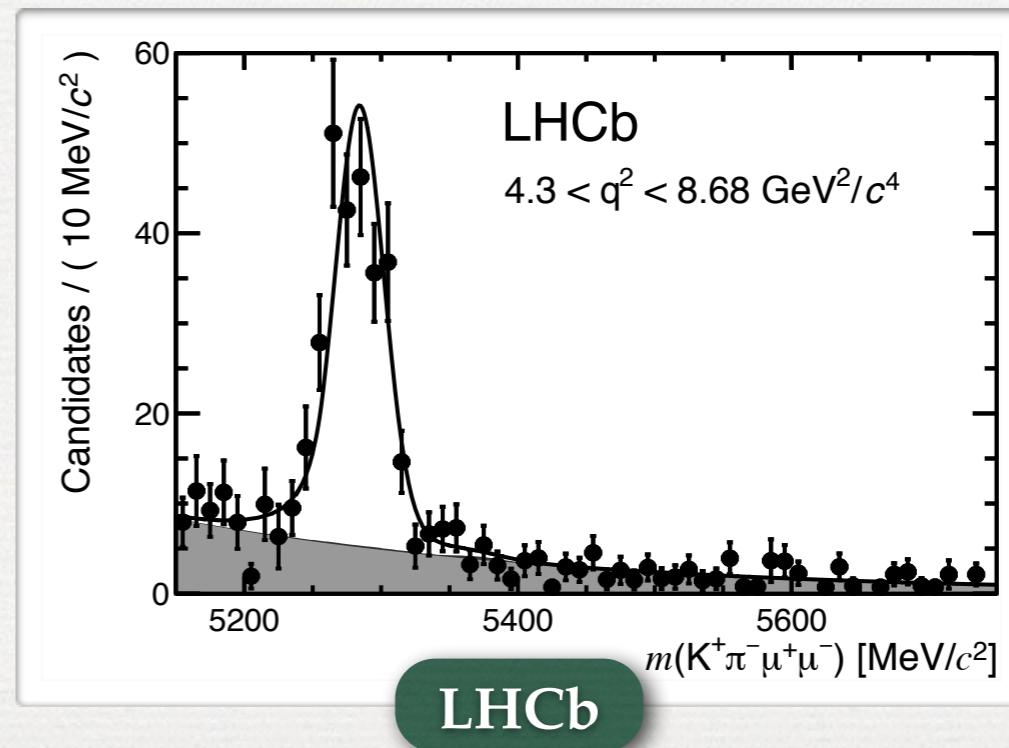
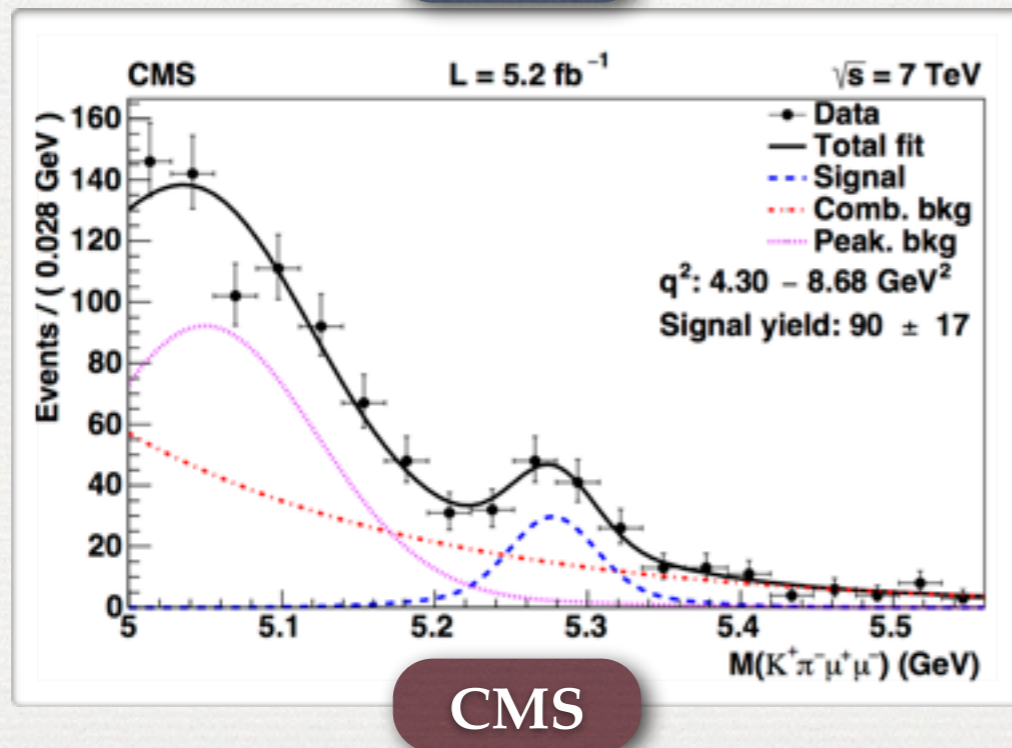
# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ EVENTS

- Clear signals have been reconstructed in bins of  $q^2$ ! (plots are from an example bin of  $4.30 < q^2 < 8.68 \text{ GeV}^2$ )



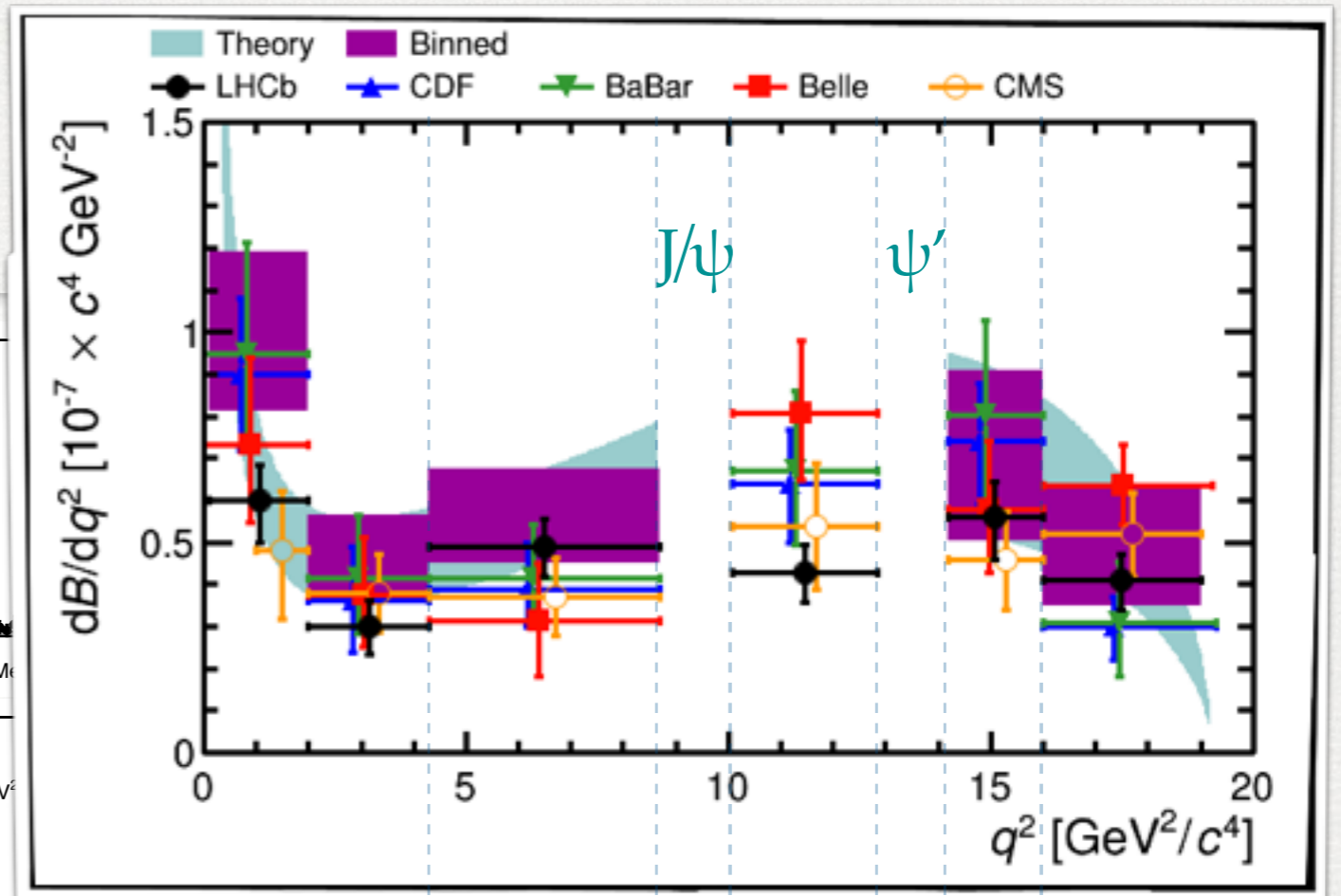
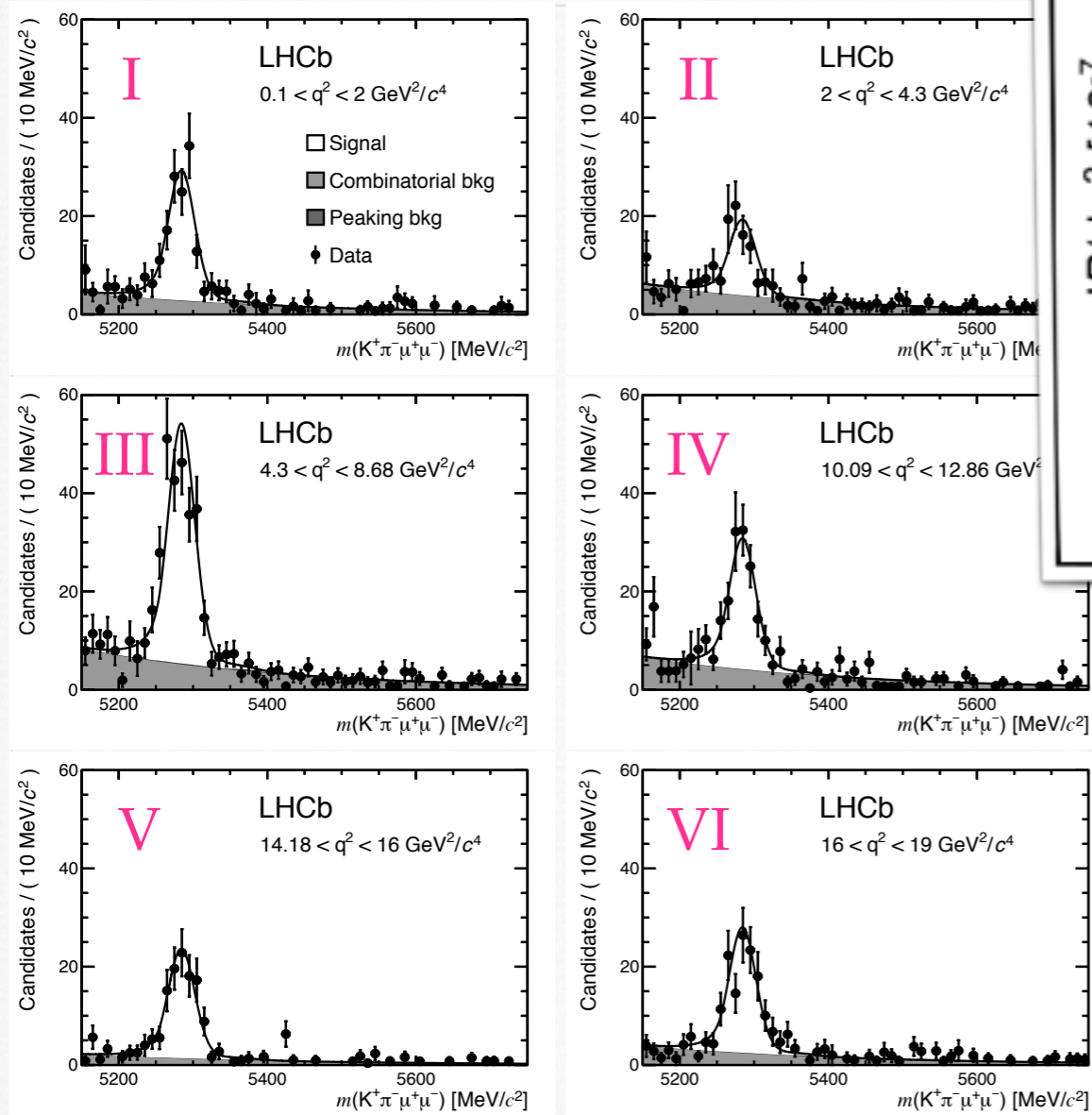
	ATLAS	CMS	LHCb
Luminosity	5 fb <sup>-1</sup>	5 fb <sup>-1</sup>	1 fb <sup>-1</sup>
Yields (tot.)	466±34	415±29	2361±56

Ref. ATLAS-CONF-2013-038  
 CMS PLB 727 (2013) 77  
 LHCb JHEP 08 (2013) 131



# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ EVENTS

Bin-by-bin on  $q^2$  yield extraction  
(take LHCb has an example)

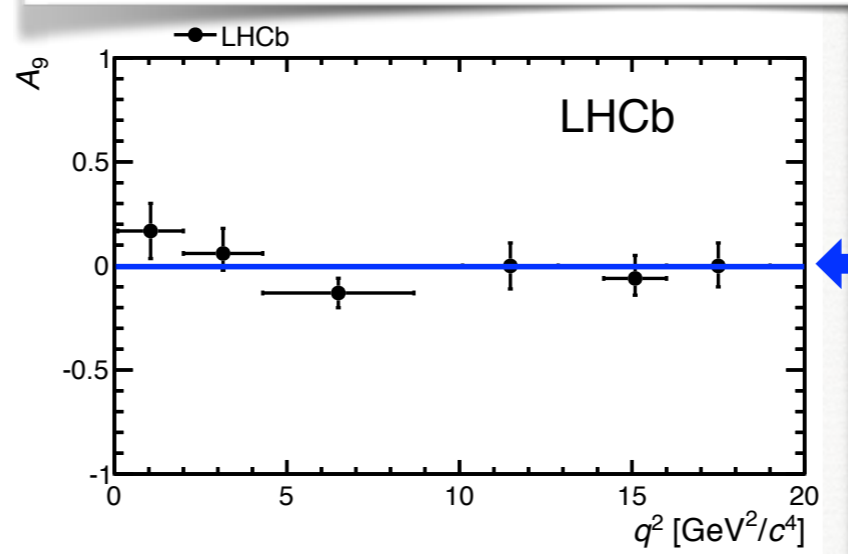
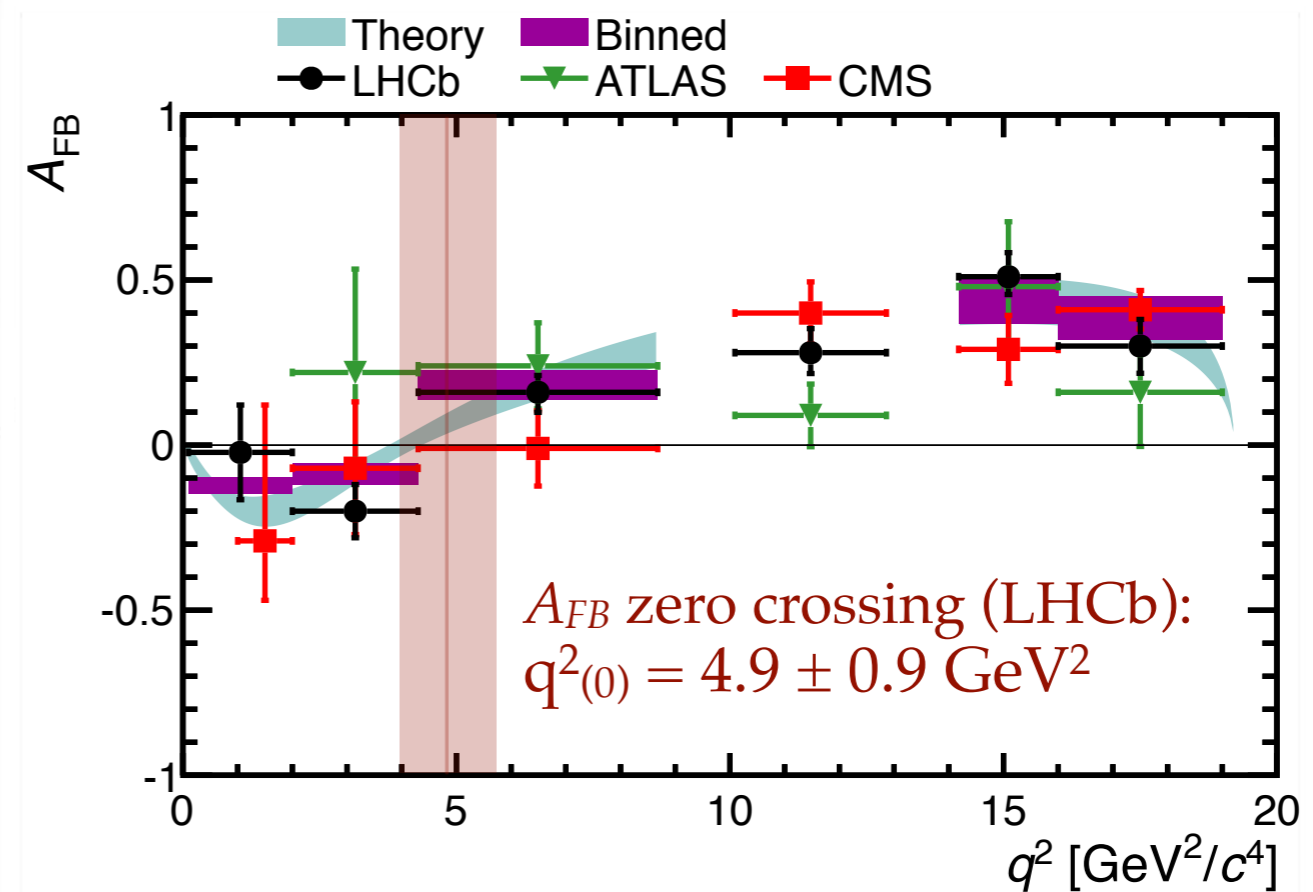
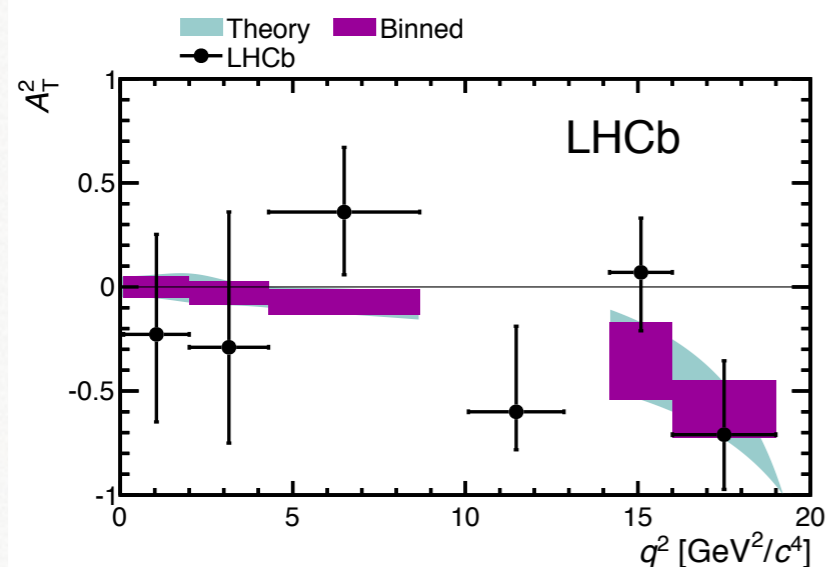
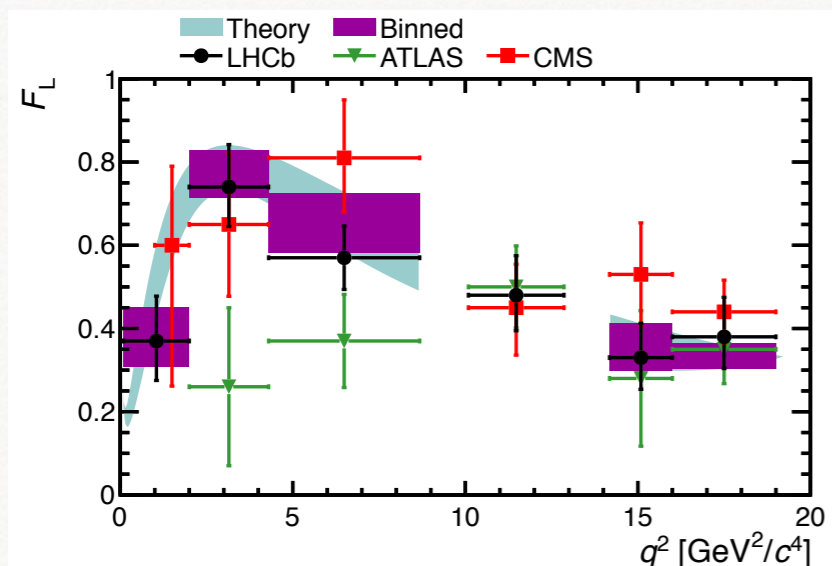


I II III IV V VI

- The differential cross sections are in agreement with the prediction.
- The events in the  $J/\psi$  and  $\psi'$  regions are used as control channel.

# ANGULAR ANALYSIS

Extract physics parameters from likelihood fits to the angular distributions.



*More or less consistent with SM...*

Ref. for TH bands:  
Bobeth et al. JHEP 07 (2011) 067

(The  $A_T$  and  $A_9$  can only be measured with the full model introduced by LHCb)



# NEW OBSERVABLES

- Apply different folding to the angular distributions to access remaining parameters.
- Newly proposed observables designed to cancel the leading form factor uncertainties.

e.g. 
$$P'_{4,5} = \frac{S_{4,5}}{\sqrt{F_L(1 - F_L)}}$$

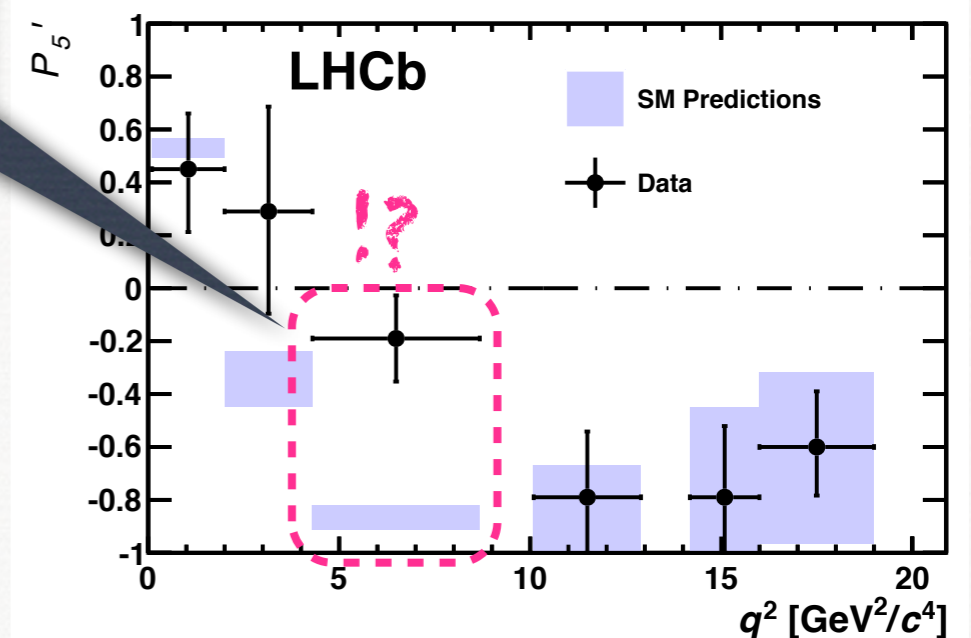
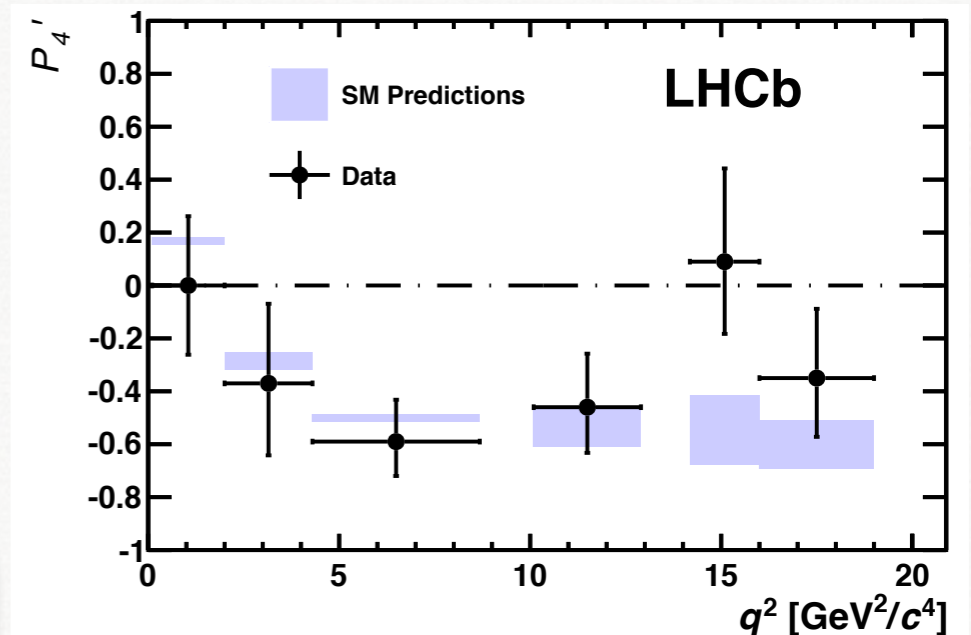
**3.7 $\sigma$**  discrepancy in  $4.3 < q^2 < 8.68 \text{ GeV}^2$  bin  
Including the look elsewhere effect (LEE):  
**~0.5% probability (2.8 $\sigma$ )**

- Simply statistical fluctuation?
- Theory error underestimated?
- New physics?  
(SUSY is difficult,  $Z'$  might work, etc.)

**➔ Check with more data/channels!**

Ref. LHCb PRL 111, 191801 (2013)

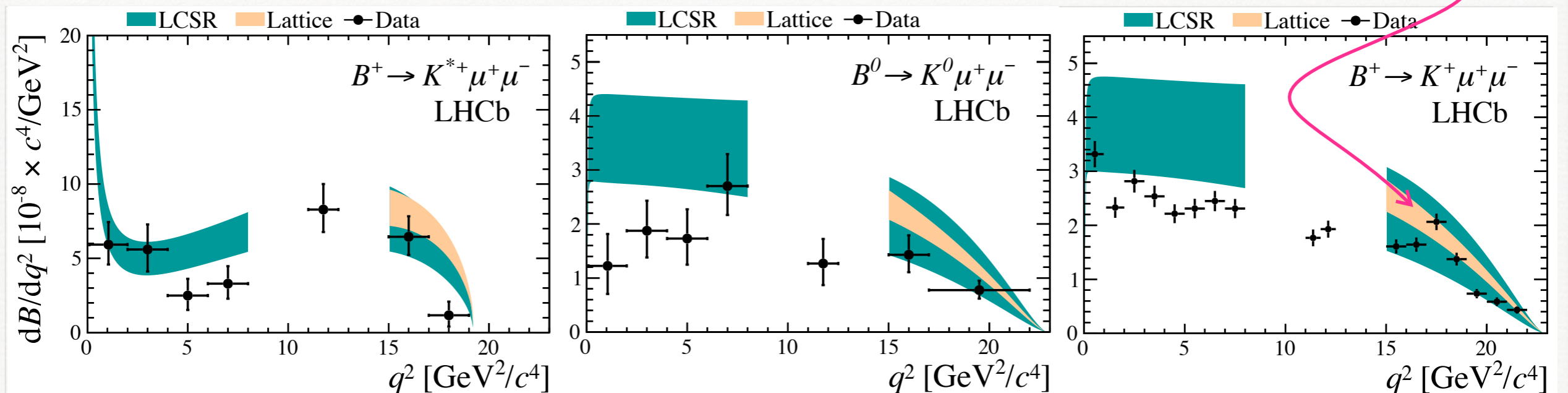
Decotes-Genon et al. JHEP 05 (2013) 137



# OTHER $B \rightarrow K^{(*)} \mu^+ \mu^-$ DECAYS

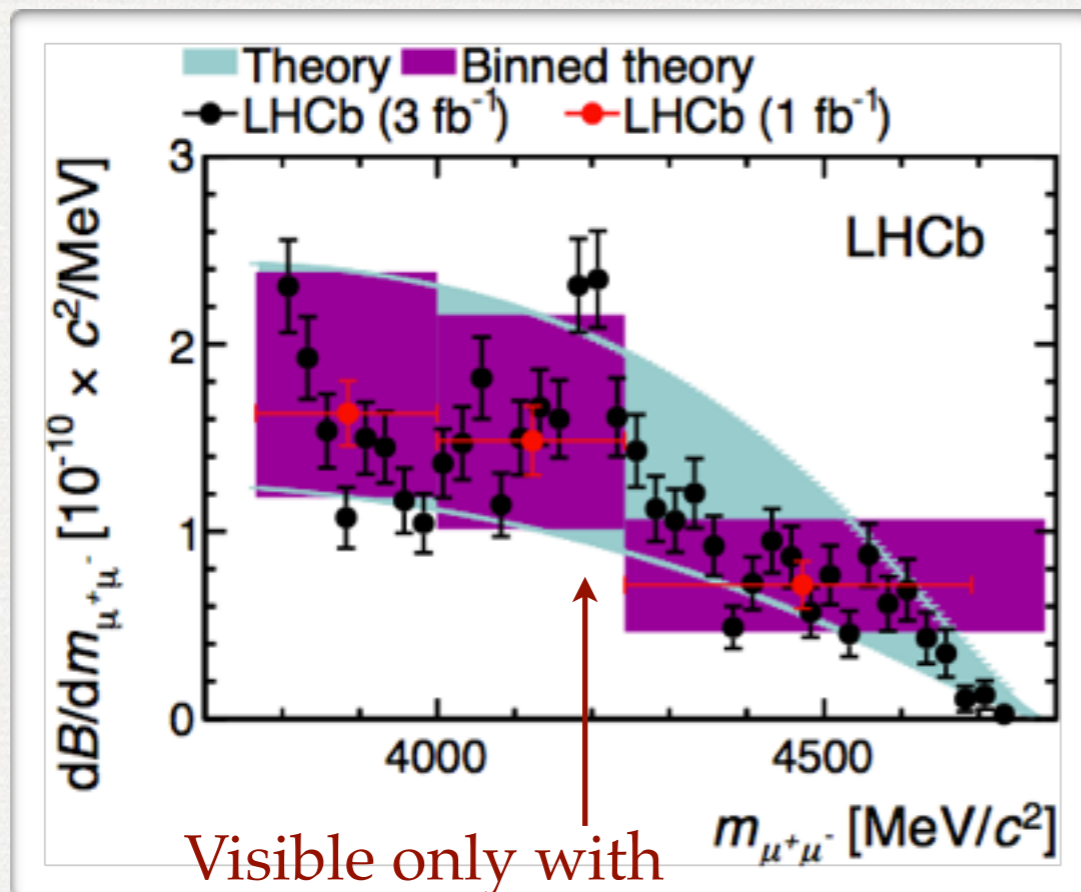
- In addition to  $K^{*0} \mu \mu$ , other channels with  $K^+$ ,  $K_S$ ,  $K^{*+}$  are also studied:
  - Channels with  $K_S$  are more challenging due to the long lifetime.
  - Clear signal observed in all channels by LHCb; differential branching fractions are normalized by  $B \rightarrow J/\psi K^{(*)}$ .
- Measurements of differential branching fractions consistently below SM
  - However the SM calculations are under revision.
- Measured isospin asymmetries are consistent with SM.

Ref. LHCb JHEP 06 (2014) 133

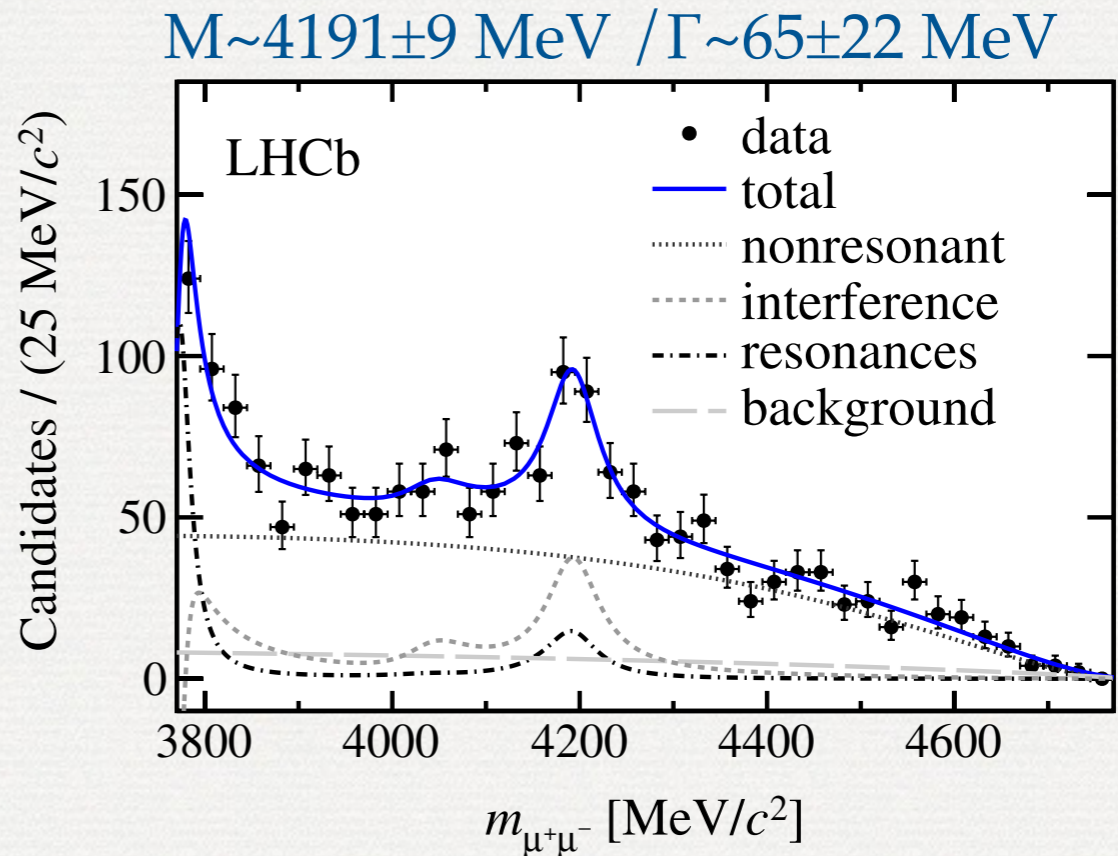


# RESONANCE IN $B^+ \rightarrow K^+ \mu\mu$ DECAYS

- Sometimes an unexpected discovery may simply “pop-up” from the experimental data!
  - Observation of a resonance structure at high  $q^2$ , which is from  $B^+ \rightarrow \psi(4160)K^+$  decay [first observation of this channel].
  - Non-trivial influence for the understanding of  $b \rightarrow s \ell \ell$  decays.



Visible only with  
large statistics!



# LEPTON UNIVERSALITY

- In the Standard Model, couplings to all leptons are universal – one can test the **lepton universality** by measuring:

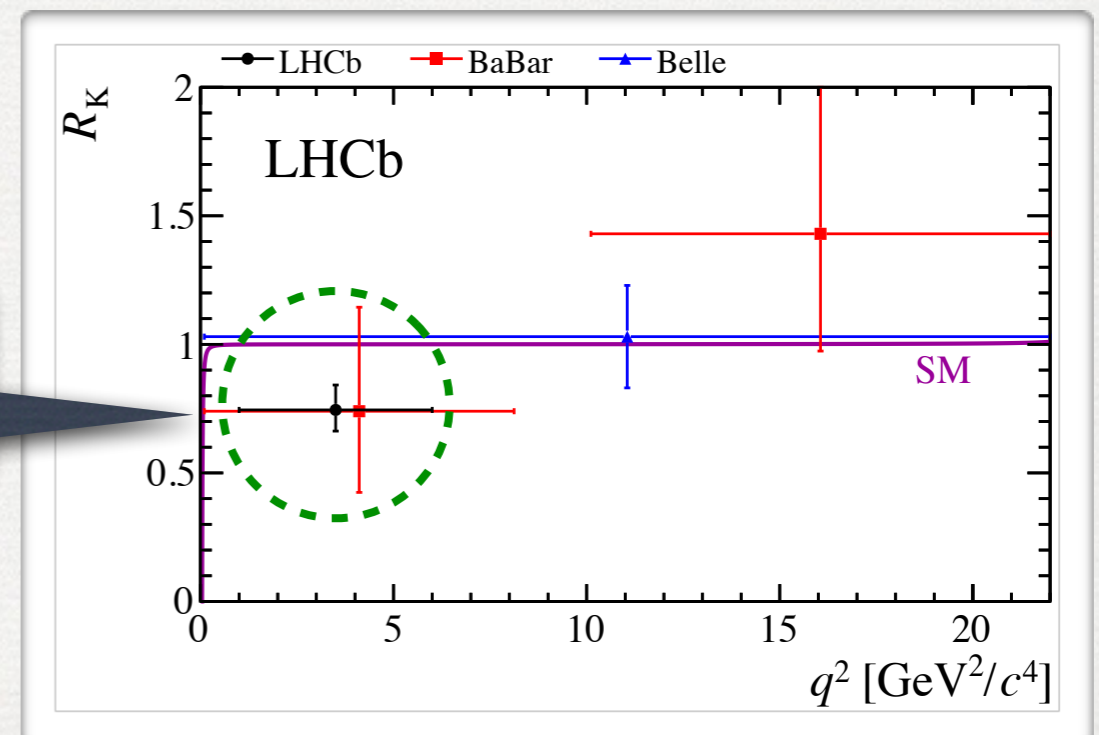
$$R_K = \frac{\int \frac{d\Gamma}{dq^2} [B^+ \rightarrow K^+ \mu^+ \mu^-] dq^2}{\int \frac{d\Gamma}{dq^2} [B^+ \rightarrow K^+ e^+ e^-] dq^2} \quad \text{In SM: } R_K(1 < q^2 < 6) \sim 1 \pm \mathcal{O}(10^{-3})$$

- Measuring  $B^+ \rightarrow K^+ e^+ e^-$  is challenging due to the bremsstrahlung radiation of the electrons.
  - Correct for bremsstrahlung with calorimeter photons.
  - double-ratio with  $B^+ \rightarrow J/\psi(e^+e^-)K^+$ .

Ref. LHCb arXiv:1406.6482

LHCb measures w/  $3\text{fb}^{-1}$  data  
 $R_K(1 < q^2 < 6) = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{syst})$

Compatible with SM prediction within  $2.6\sigma$ .

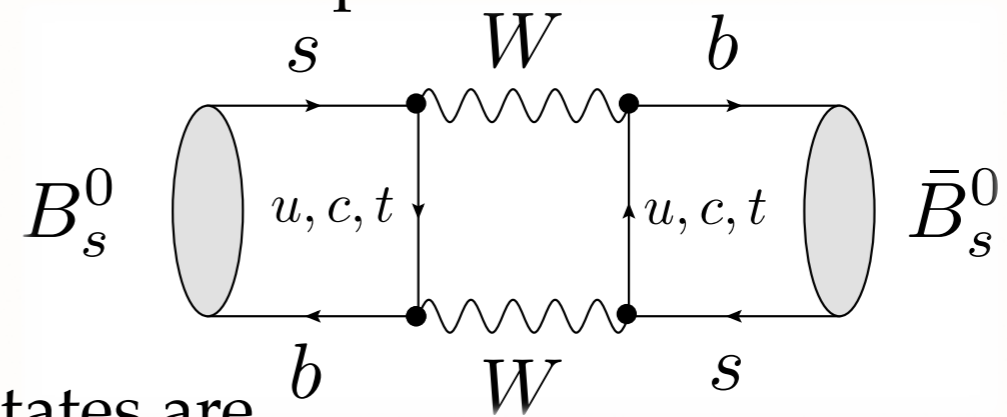


# B<sub>s</sub> MIXING

- Neutral B<sub>s</sub> mesons show the quantum-mechanical phenomenon of “mixing” with presence of the box diagram.
- Produced B<sub>s</sub> meson state evolves with a time-dependent linear combination of two eigenstates.

$$|B_H\rangle = p|B_s\rangle - q|\bar{B}_s\rangle$$

$$|B_L\rangle = p|B_s\rangle + q|\bar{B}_s\rangle$$



- The “heavy” and “light” mass eigenstates are characterized by:

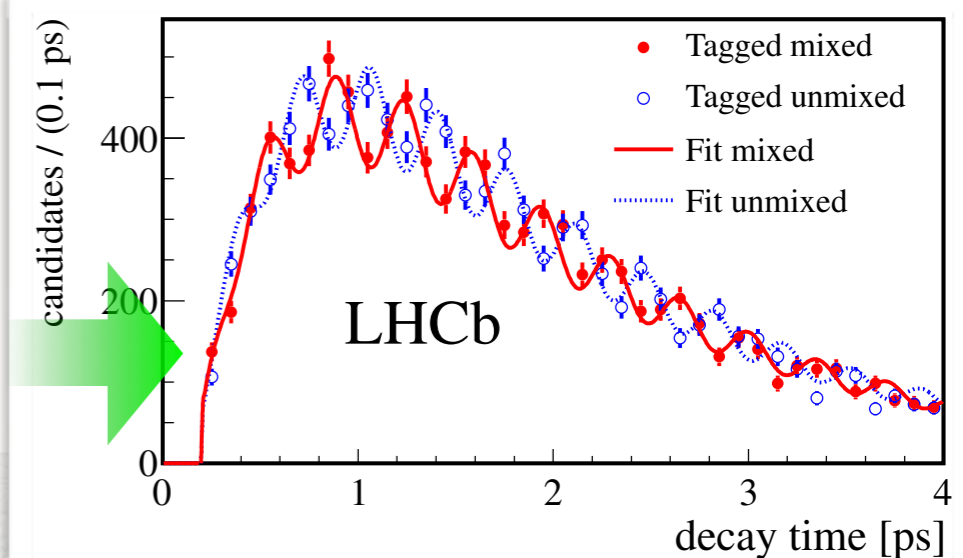
Mass difference:  $\Delta m_s \equiv M_H - M_L$

Decay width difference:  $\Delta \Gamma_s \equiv \Gamma_L - \Gamma_H$

Oscillation frequency proportion to  $\Delta m_s \sim 17.768 \pm 0.023 \pm 0.006 \text{ ps}^{-1}$

Ref. LHCb NJP 15 (2013) 053021

A perfect QM 2-state demo!

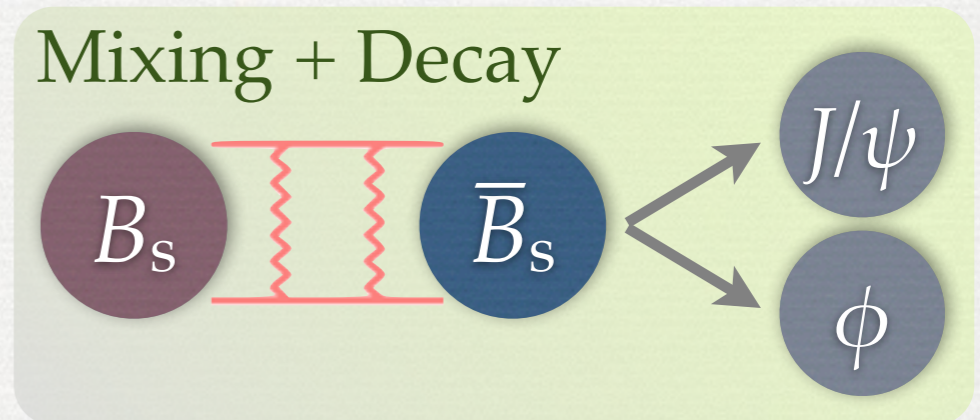


# CP VIOLATION IN $B_s$ MIXING

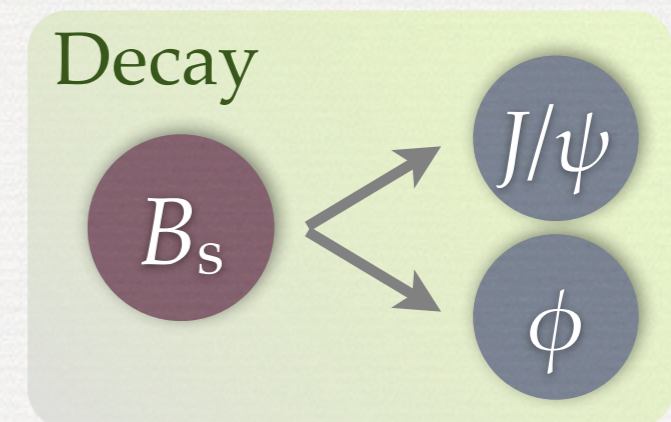
- When  $B_s$  and anti- $B_s$  decay to exactly the same final state (e.g.  $B_s \rightarrow J/\psi \phi$ ), the **weak phase  $\phi_s$**  arises from the interference between direct decays and decays with mixing.
- The amplitude of CP violation  $\propto \sin\phi_s$ , where

$$\phi_s \approx -2\beta_s, \quad \beta_s = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*)$$

**in SM  $\phi_s \approx (-0.0363^{+0.0016}_{-0.0015})$  rad**



+ quantum interference



- Many **new physics scenarios** may enhance the value of  $\phi_s$ .
- Experimentally clean — the final states can be fully reconstructed with small background.

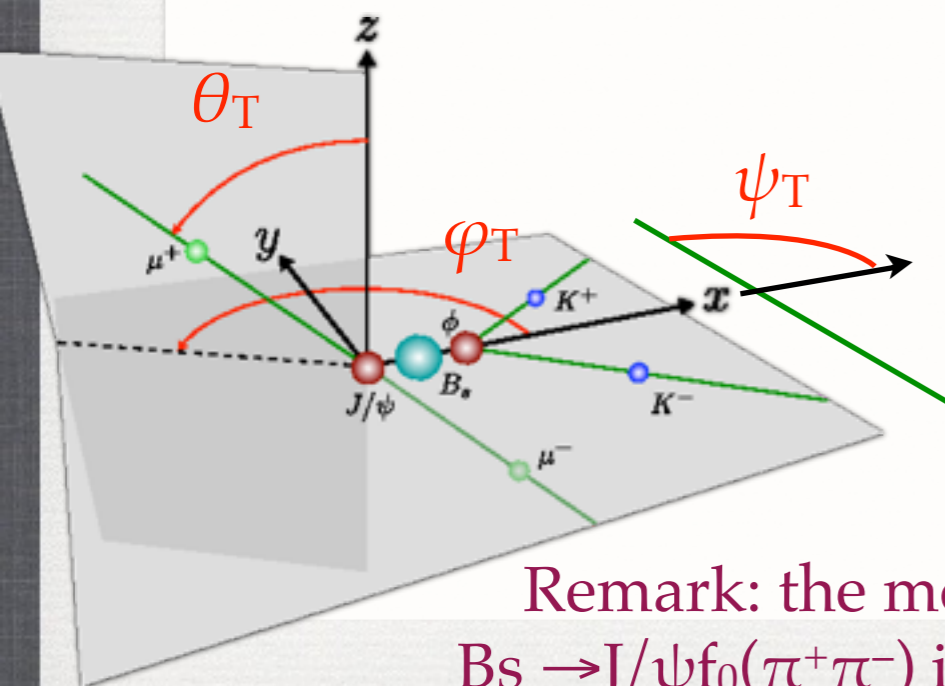
# ANALYSIS OF $B_s \rightarrow J/\psi\phi$

- Two vector mesons in the final state – an admixture of CP states.
- Angular analysis is introduced to disentangle CP-odd and CP-even components.

- A complex model: 
$$\frac{d^4\Gamma[B_s(t)]}{d\Theta dt} = \sum_{i=1}^{10} \mathcal{O}_i(\alpha, t) \cdot g_i(\Theta)$$

$$\mathcal{O}_i(\alpha, t) \propto e^{-\Gamma_s t} \left[ a_i \cosh\left(\frac{1}{2}\Delta\Gamma_s t\right) + b_i \sinh\left(\frac{1}{2}\Delta\Gamma_s t\right) + c_i \cos(\Delta m_s t) + d_i \sin(\Delta m_s t) \right]$$

Proportional to  $\sin\phi_s$  or  $\cos\phi_s$   
(see the reference below for the full model)



$\alpha$ : physics parameters to be determined, include  $\phi_s, \Delta\Gamma_s, \Gamma_s, \dots$

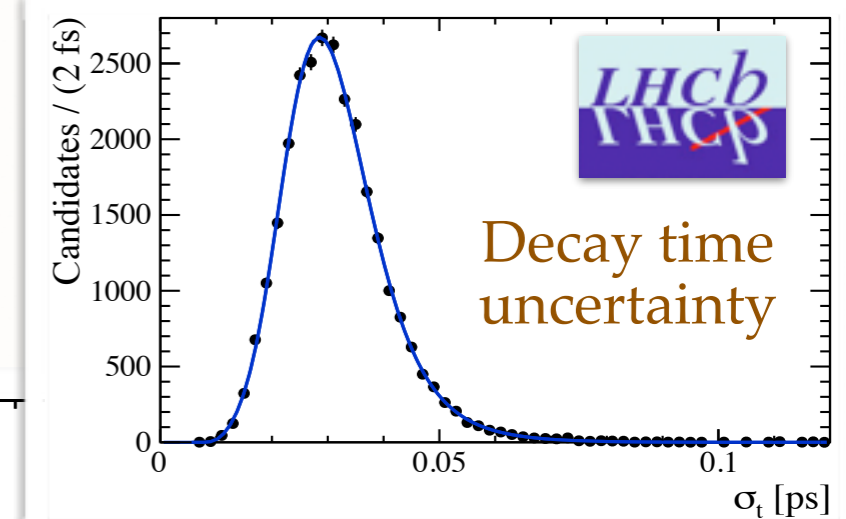
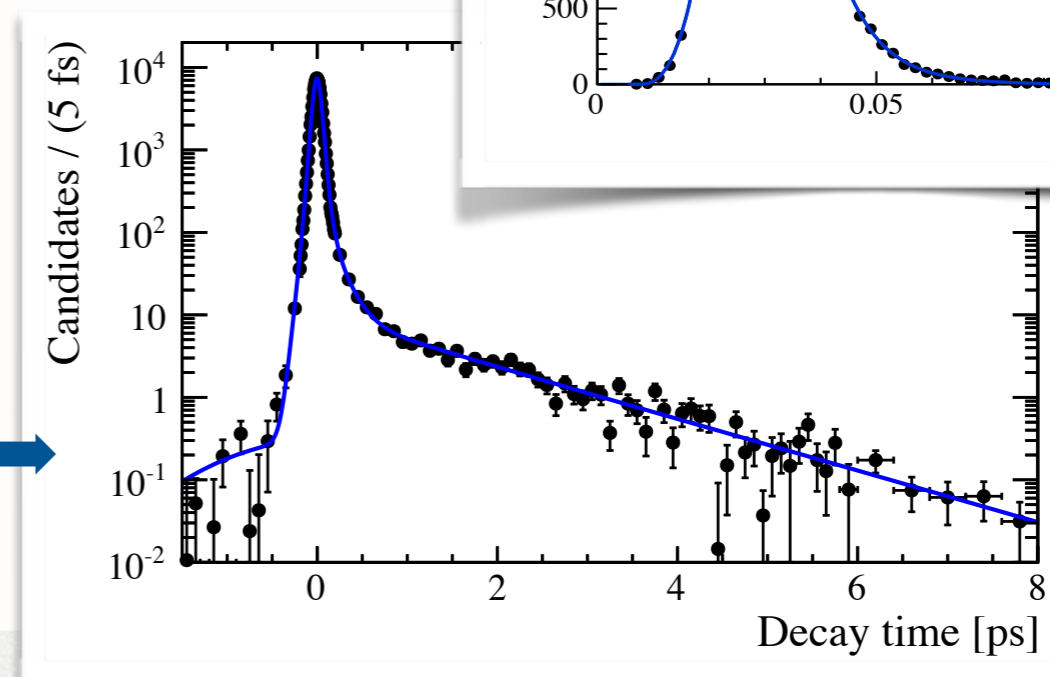
$\Theta$ : decay angles, either in **transversity bases** (left fig.), or **helicity bases** (similar to  $K^*\mu\mu$ )

Remark: the model for  $B_s \rightarrow J/\psi f_0(\pi^+\pi^-)$  is simpler!

# EFFICIENCY & RESOLUTION

- Key elements for the measurement: **decay time resolution** and **angular efficiency** modeling.
- Angular efficiency can be modeled with a 3D function of decay angles.
- Decay time resolution is estimated from  **$B_s$  decay vertex finding** for each candidate and is included in the final fit convoluted with a Gaussian-type resolution function.
  - ATLAS:  $\sim 90$  fs
  - CMS:  $\sim 70$  fs
  - LHCb:  $\sim 45$  fs

Without resolution one should see a  $\delta$ -function  $\sim 0$  (prompt  $J/\psi$  background) and simple exponential to the right (=straight line in log scale)

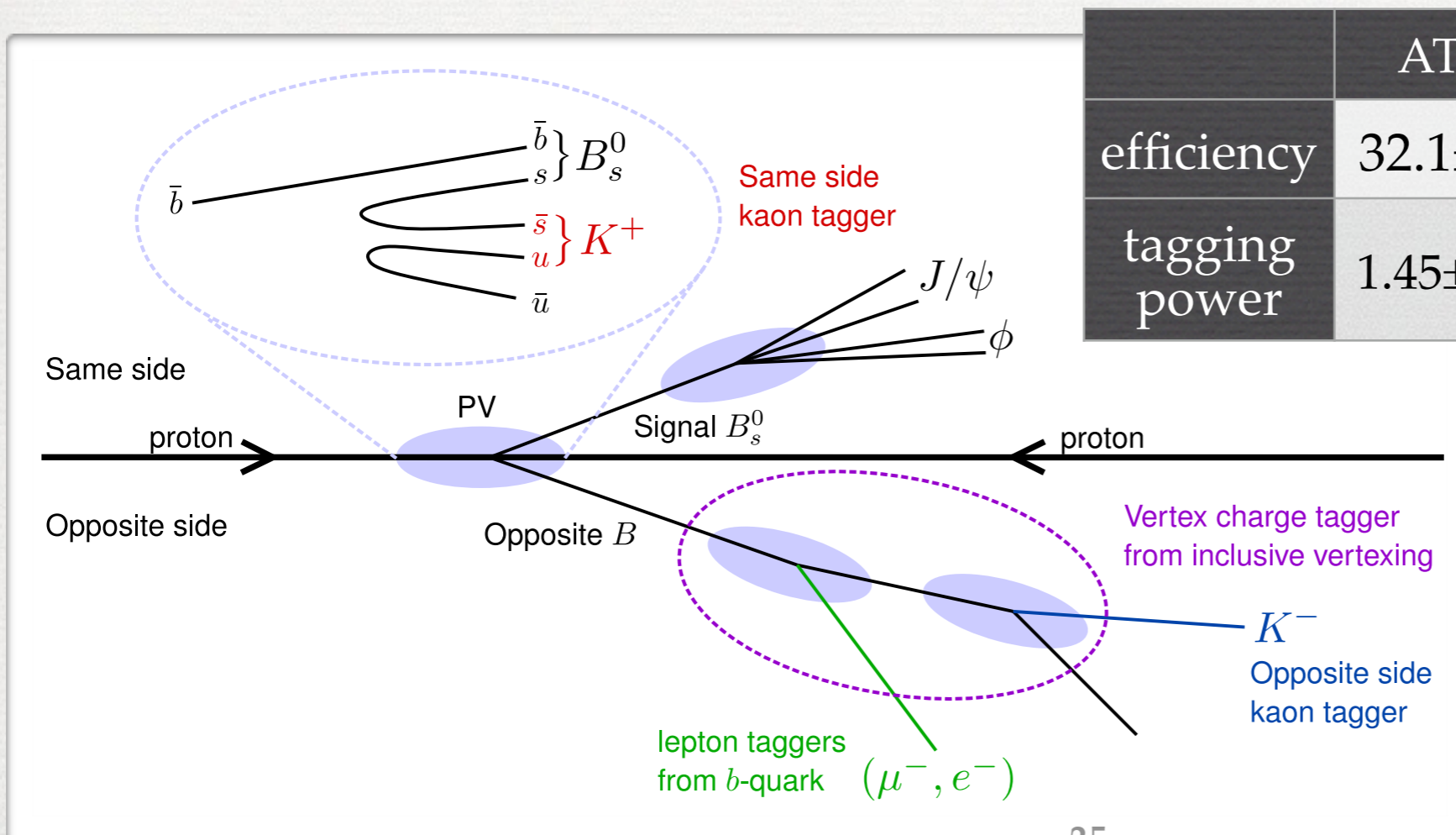




# FLAVOUR TAGGING

- **Flavour tagging** is another essential piece of the analysis.
- Determination for the flavour of the  $B_s$  meson at production with
  - opposite-side tagging (OST): partial reconstruction of another  $b$  hadron in the event.
  - same-side tagging (SST): identify the residual strange quark associated with  $B_s$  meson production.

Tagging power =  
efficiency  $\times$  (1-2 $\omega$ )  
 $\omega$ : wrong tag fraction



	ATLAS	CMS	LHCb
efficiency	$32.1 \pm 0.1\%$	$7.67 \pm 0.04\%$	$39.4 \pm 0.3\%$
tagging power	$1.45 \pm 0.05\%$	$0.97 \pm 0.04\%$	$3.13 \pm 0.23\%$

ATLAS: OST( $\mu$  + jet change)

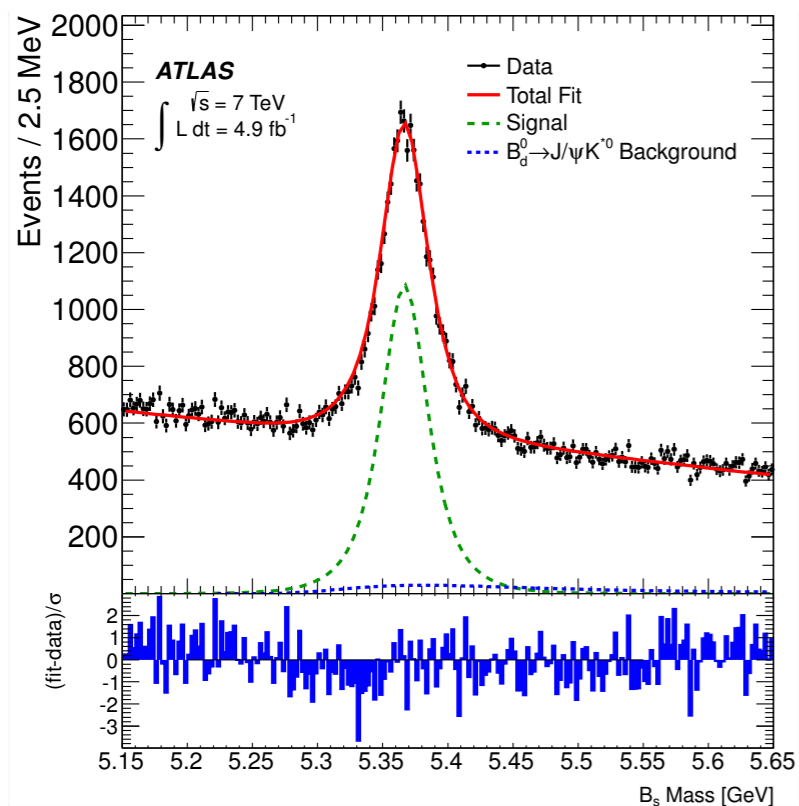
CMS: OST( $\mu$  +  $e$ )

LHCb: OST(all) + SST

# CANDIDATE EVENTS

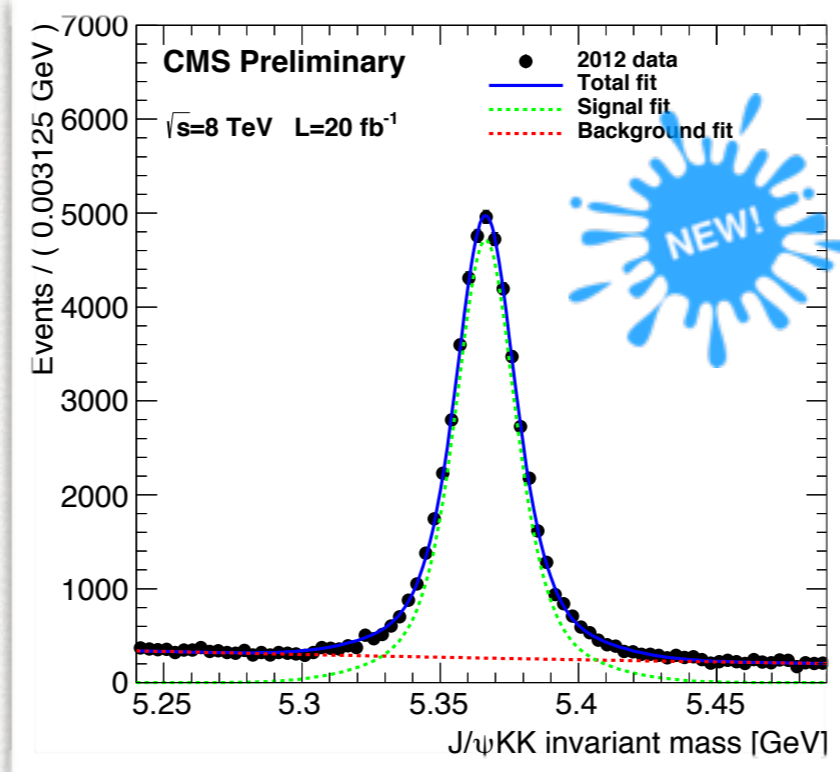
- All with clean signals!
- Likelihood fits applied to extract the yields.

Ref. ATLAS JHEP 12 (2012) 072



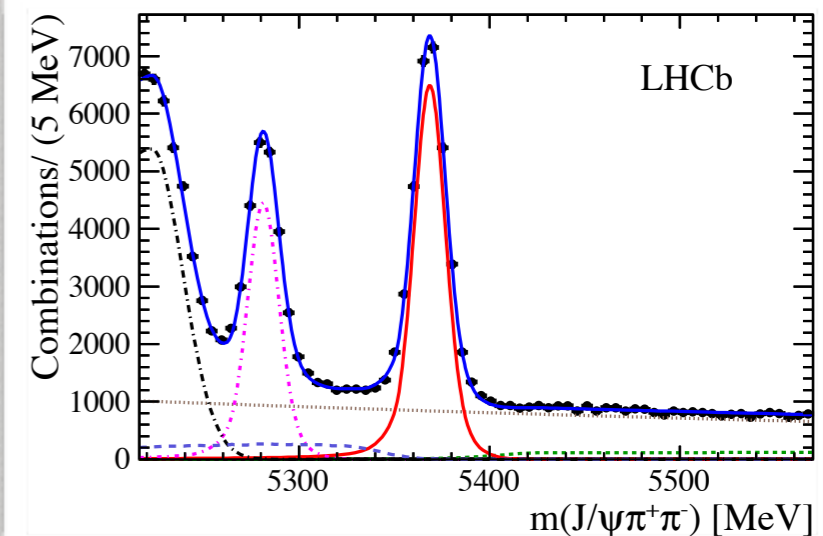
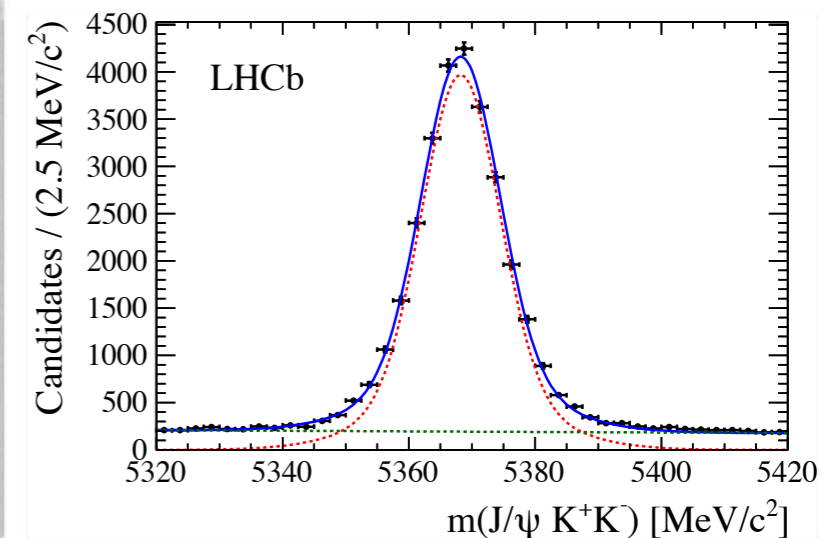
**ATLAS  $5 \text{ fb}^{-1}$**   
 $N(B_s) = 22690 \pm 160$

Ref. CMS PAS BPH-13-012



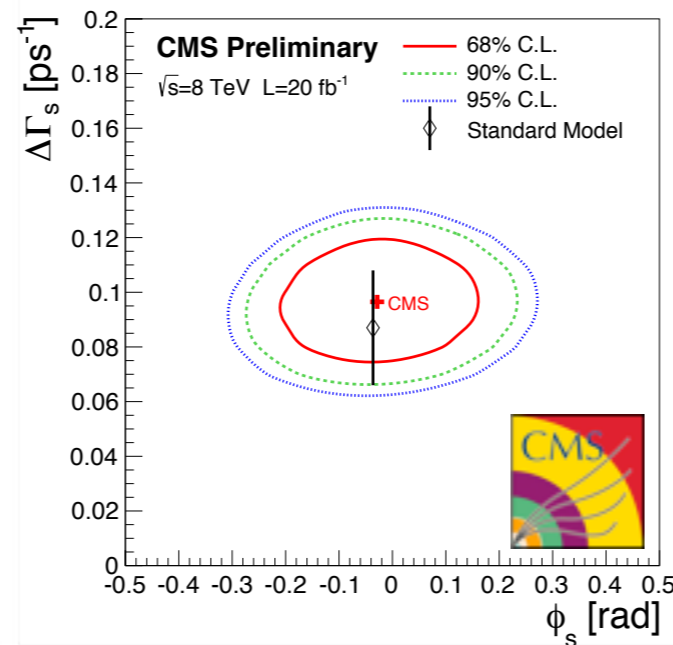
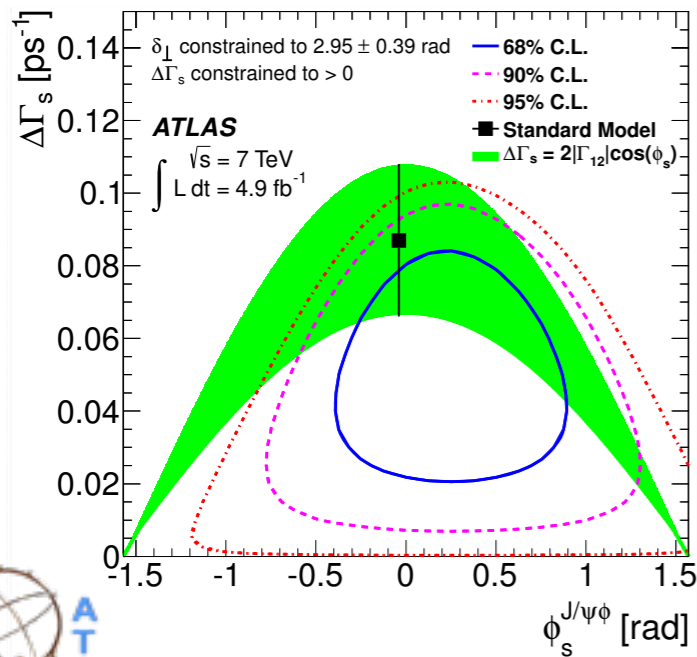
**CMS  $20 \text{ fb}^{-1}$**   
 $N(B_s) \sim 49000$

Ref. LHCb PRD 87, 112010 (2013)  
 LHCb arXiv:1405.4140



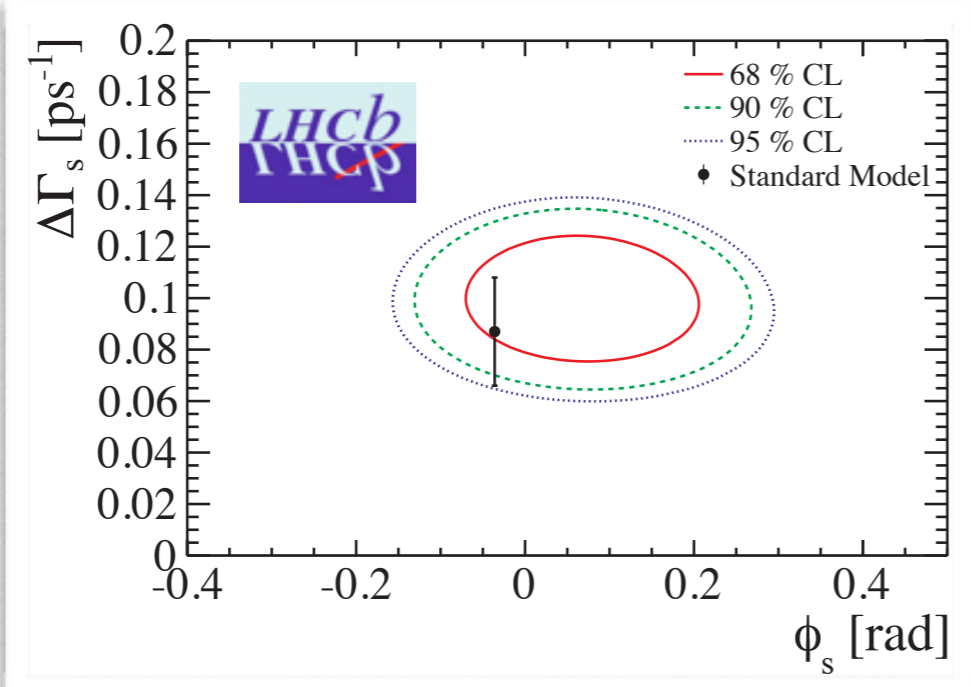
**LHCb**  
 $N(B_s \rightarrow J/\psi KK) = 27617 \pm 115 @ 1 \text{ fb}^{-1}$   
 $N(B_s \rightarrow J/\psi \pi\pi) \sim 27100 @ 3 \text{ fb}^{-1}$

# EXTRACTION OF $\phi_s$ & $\Delta\Gamma_s$



**ATLAS 5 fb<sup>-1</sup>**  
 $\phi_s = 0.12 \pm 0.25 \pm 0.05 \text{ rad}$   
 $\Delta\Gamma_s = 0.053 \pm 0.021 \pm 0.10 \text{ ps}^{-1}$

**CMS 20 fb<sup>-1</sup>**  
 $\phi_s = -0.03 \pm 0.11 \pm 0.03 \text{ rad}$   
 $\Delta\Gamma_s = 0.096 \pm 0.014 \pm 0.007 \text{ ps}^{-1}$



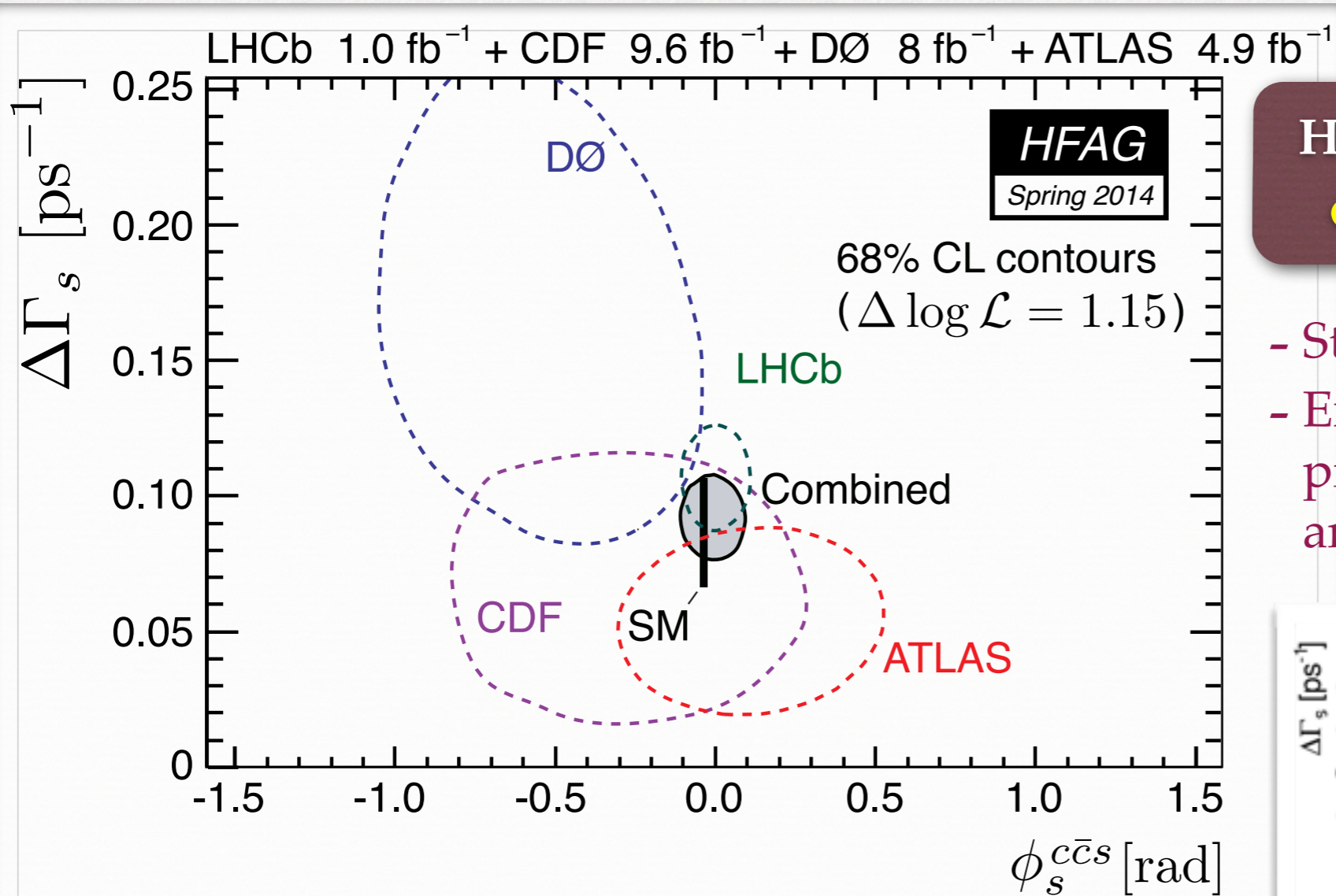
**LHCb  $B_s \rightarrow J/\psi KK$  @ 1 fb<sup>-1</sup>**  
 $\phi_s = 0.07 \pm 0.09 \pm 0.01 \text{ rad}$   
 $\Delta\Gamma_s = 0.100 \pm 0.016 \pm 0.003 \text{ ps}^{-1}$

**LHCb  $B_s \rightarrow J/\psi \pi\pi$  @ 3 fb<sup>-1</sup>**  
 $\phi_s = 0.075 \pm 0.067 \pm 0.008 \text{ rad}$   
**LHCb combination**  
 $\phi_s = 0.070 \pm 0.055 \text{ rad}$



# $\phi_s / \Delta\Gamma_s$ COMBINATION: $B_s \rightarrow J/\psi\phi$

Ref. [http://www.slac.stanford.edu/xorg/hfag/osc/spring\\_2014/](http://www.slac.stanford.edu/xorg/hfag/osc/spring_2014/)

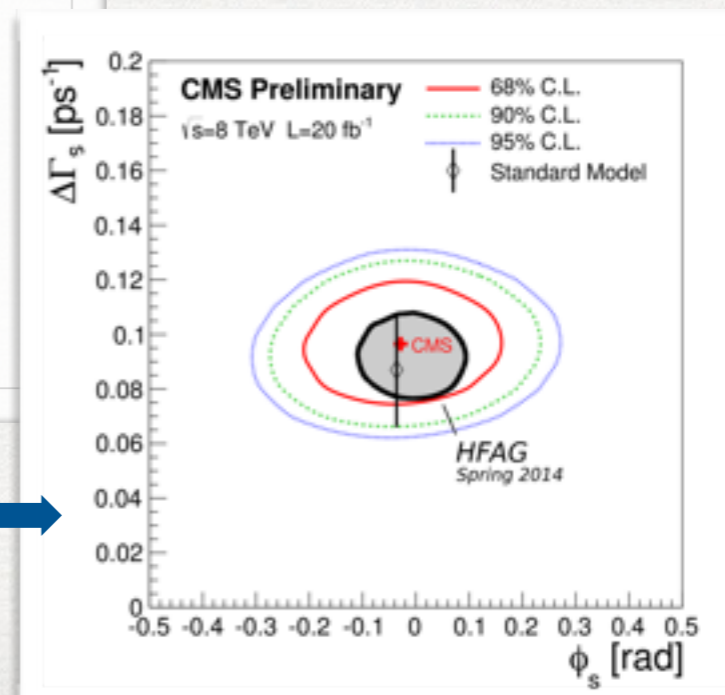


HFAG Spring 2014 Average

$$\phi_s = +0.00 \pm 0.07 \text{ rad}$$

- Still statistics dominant.
- Expected to improve the precision with new CMS result and LHCb full data update.

New CMS result has not yet been included in the average. →



# SUMMARY

- Three important B-physics analyses at the LHC are discussed
  - First observation of very rare decay of  $B_s \rightarrow \mu\mu$ .
  - Extended measurements for  $B \rightarrow K^{(*)} \mu\mu$  decays.
  - Weak phase  $\phi_s$  measured through the  $B_s \rightarrow J/\psi\phi$  decays.
- B-physics studies play an important role for the search of physics beyond the SM. No striking signal yet, but some tensions do emerge. More data will help to clarify them.
- Topics which are not covered:
  - Many b-hadron production, decay, and property measurements.
  - Quarkonia measurements and exotic quarkonia searches.



# BACKUP SLIDES